# lecture 10: image retrieval and manifold learning deep learning for vision

Yannis Avrithis

Inria Rennes-Bretagne Atlantique

Rennes, Nov. 2018 - Jan. 2019



#### outline

background pooling manifold learning fine-tuning graph-based methods

## background

#### image classification challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting

- number of instances
- texture/color
- pose
- deformability
- intra-class variability



#### image classification challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting

- number of instances
- texture/color
- pose
- deformability
- intra-class variability



#### image retrieval challenges





















- scale
- viewpoint
- occlusion
- clutter
- lighting

- distinctiveness
- distractors

main difference to classification:

no intra-class variability

#### image retrieval challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting

- distinctiveness
- distractors

main difference to classification:

• no intra-class variability



#### image retrieval challenges





















- scale
- viewpoint
- occlusion
- clutter
- lighting

- distinctiveness
- distractors

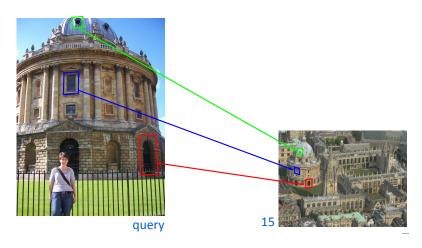
main difference to classification:

• no intra-class variability

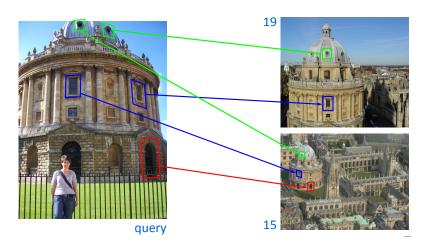


query

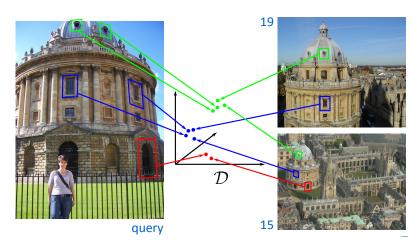
• query vs. dataset image



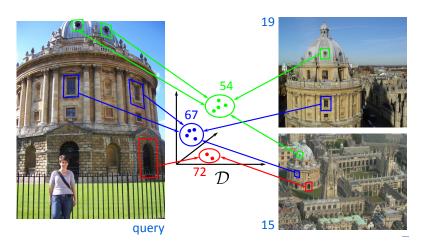
• pairwise descriptor matching



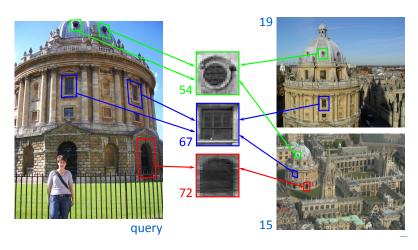
• pairwise descriptor matching for every dataset image



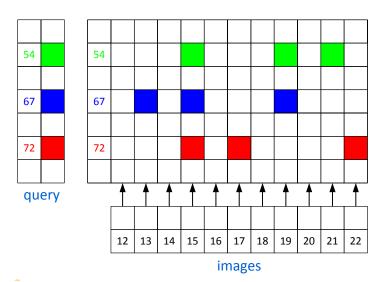
similar descriptors should all be nearby in the descriptor space



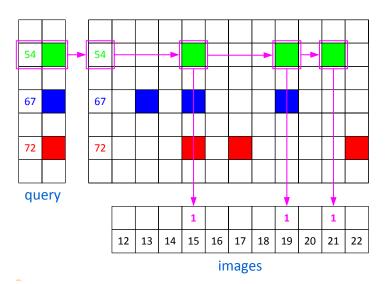
• let's quantize them into visual words



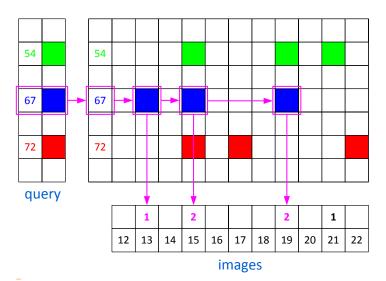
now visual words act as a proxy; no pairwise matching needed



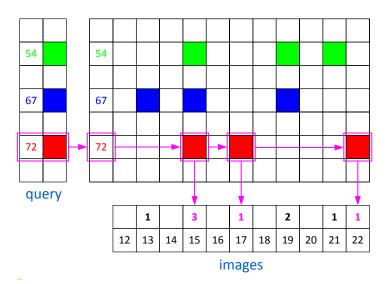




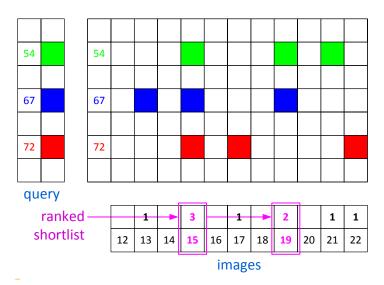






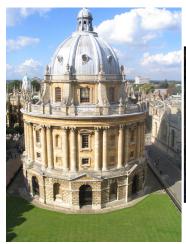








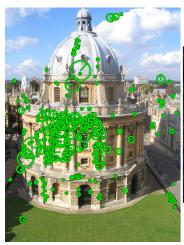






original images

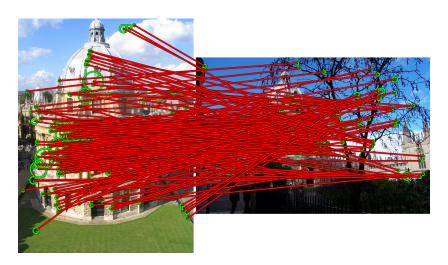






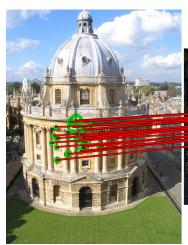
#### local features





tentative correspondences: too many







inliers: now more expensive to find



#### application: location and landmark recognition



PEstimated Location Similar Image, Incorrectly geo-tagged Unavailable



Suggested tags: Buxton Memorial Fountain, Victoria Tower Gardens, London Frequent user tags: Victoria Tower Gardens, Buston Memorial Fountain, Winchester Palace, Architecture, Victorian gothic

#### Similar Images



Original ••



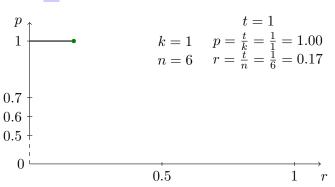
Similarity: 0.491 Original ••



Similarity: 0.397 Original ••

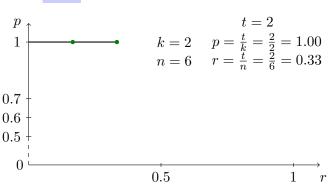


Original ••



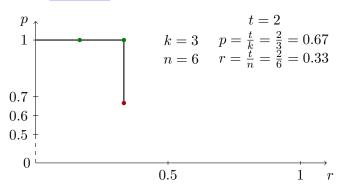
- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$





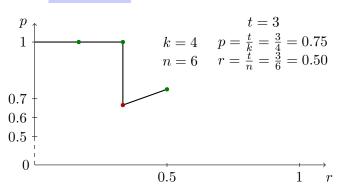
- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$





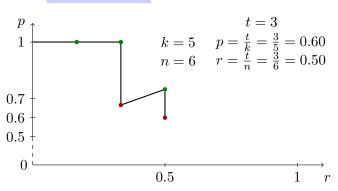
- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$





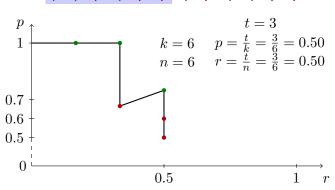
- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$





- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$



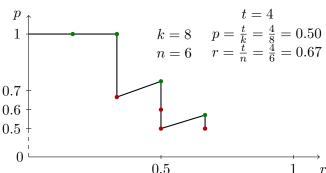


- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$



- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$



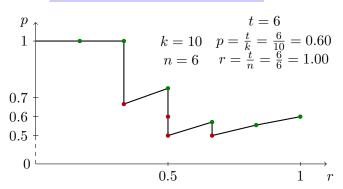


- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$



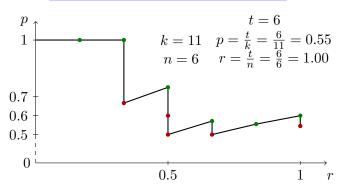
- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$





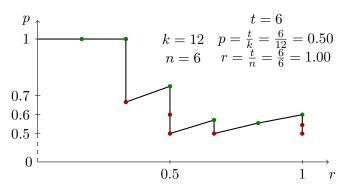
- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$





- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$





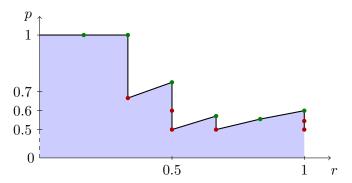
- # total ground truth n, current rank k, # true positives t
- precision  $p = \frac{t}{k}$ , recall  $r = \frac{t}{n}$



# average precision (AP)

ranked list of items with true/false labels

1 2 3 4 5 6 7 8 9 10 11 12 T T F T F F T F T T F F



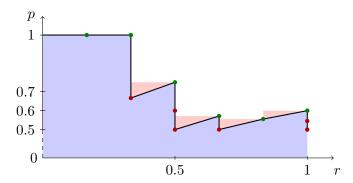
- average precision = area under curve
- the mean average precision (mAP) is the mean over queries



# average precision (AP)

ranked list of items with true/false labels

1 2 3 4 5 6 7 8 9 10 11 12 T T F T F F T F T T F F



- average precision = area under curve (filled-in curve)
- the mean average precision (mAP) is the mean over queries



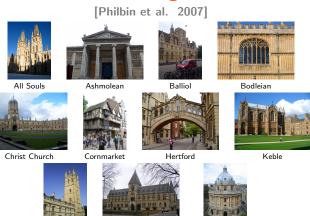
#### Holidays dataset

[Jégou et al. 2008]



- personal holiday photos, natural and man-made scenes
- 1.5k images, 500 groups, 1 query/group, 1000 positives,  $1\sim 12$  positives/query

#### Oxford buildings dataset



• Oxford5k: 5k images, 11 landmarks,  $5 \times 11 = 55$  queries,  $10 \sim 200$  positives/query

Radcliffe Camera

Pitt Rivers

Oxford105k: 100k additional distractor images

Magdalen

#### Paris dataset

[Philbin et al. 2008]



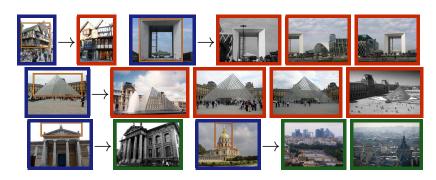
- Paris6k: 6k images, 11 landmarks,  $5 \times 11 = 55$  queries,  $50 \sim 300$  positives/query
- Paris106k: same 100k distractor images as Oxford

Philbin, Chum, Isard, Sivic and Zisserman. CVPR 2008. Lost in Quantization: Improving Particular Object Retrieval in Large Scale Image Databases.



#### Oxford and Paris revisited

[Radenović et al. 2018]



- re-labeling to correct annotation mistakes
- new queries added, 70 queries in total per dataset
- easy/medium/hard evaluation protocol
- 1M hard distractor images

# aggregated selective match kernel (ASMK)\*

[Tolias et al. 2013]

residual pooling within cells

$$V(X_c) := \sum_{x \in X_c} r(x) = \sum_{x \in X_c} x - q(x)$$

• nonlinear selectivity between cells

$$K(X,Y) := \gamma(X)\gamma(Y) \sum_{c \in C} w_c \sigma_\alpha \left( \hat{V}(X_c)^\top \hat{V}(Y_c) \right)$$

where  $\hat{x} := x/\|x\|$  and  $\sigma_{\alpha}$  a nonlinear function

# triangulation embedding (T-embedding)\*

[Jégou and Zisserman 2014]

normalized residuals, concatenated over cells, pooling over dataset

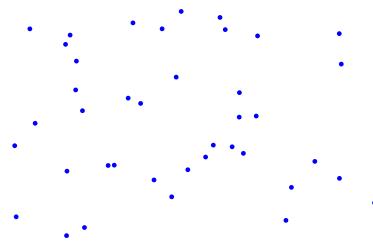
$$R(X) := \sum_{x \in X} (\hat{r}_1(x), \dots, \hat{r}_k(x)) = \sum_{x \in X} \left( \frac{x - c_1}{\|x - c_1\|}, \dots, \frac{x - c_k}{\|x - c_k\|} \right)$$

where  $r_i(x) := x - c_i$  and  $\hat{x} := x/\|x\|$ 

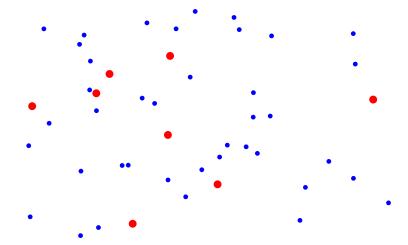
• linear kernel, written as inner product

$$K(X,Y) := (\gamma(X)R(X))^{\top} (\gamma(Y)R(Y))$$





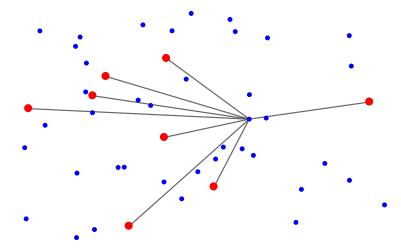
• input vectors – codebook – residuals – normalized residuals



• input vectors – codebook – residuals – normalized residuals

Jégou and Zisserman. CVPR 2014. Triangulation Embedding and Democratic Aggregation for Image Search.

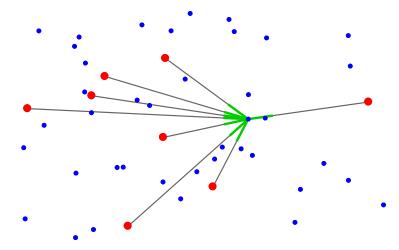




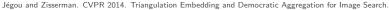
• input vectors - codebook - residuals - normalized residuals

Jégou and Zisserman. CVPR 2014. Triangulation Embedding and Democratic Aggregation for Image Search.





• input vectors – codebook – residuals – normalized residuals





#### performance

- aggregated selective match kernel
  - mAP 81.7 (83.8) mAP on Oxford5k, 78.2 (80.5) on Paris6k, 82.2 (86.5) on Holidays
  - $\sim 2.2$ k (3.8k) descriptors/image  $\times$  128 dimensions
- triangulation embedding
  - mAP 57.1 (67.6) on Oxford5k, 72.3 (77.1) on Holidays
  - global descriptor, 1920 (8064) dimensions
- no spatial verification or other post-processing

#### state of the art before deep learning

- bag of words and inverted index is only a crude form of approximate nearest neighbor search for each local descriptor, followed by a kernel function
- for good performance, storing descriptors is necessary, even compressed
- very good performance achieved with thousands descriptors/image
- a global descriptor/image allows nearest neighbor search directly on images, but is inferior

## state of the art before deep learning

- bag of words and inverted index is only a crude form of approximate nearest neighbor search for each local descriptor, followed by a kernel function
- for good performance, storing descriptors is necessary, even compressed
- very good performance achieved with thousands descriptors/image
- a global descriptor/image allows nearest neighbor search directly on images, but is inferior

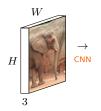
# pooling

[Krizhevsky et al. 2012]



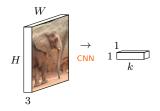
- 3-channel RGB input,  $224 \times 224$
- AlexNet pre-trained on ImageNet for classification
- last fully connected layer (fc<sub>6</sub>): global descriptor of dimension k=4096

[Krizhevsky et al. 2012]



- 3-channel RGB input,  $224 \times 224$
- AlexNet pre-trained on ImageNet for classification
- last fully connected layer (fc<sub>6</sub>): global descriptor of dimension k=4096

[Krizhevsky et al. 2012]

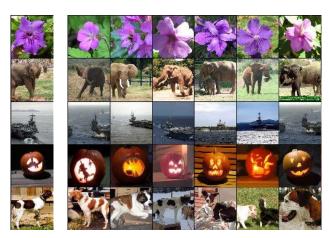


- 3-channel RGB input,  $224 \times 224$
- AlexNet pre-trained on ImageNet for classification
- last fully connected layer (fc<sub>6</sub>): global descriptor of dimension k=4096

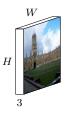




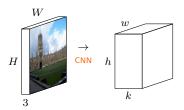
- query images
- nearest neighbors in ImageNet according to Euclidean distance



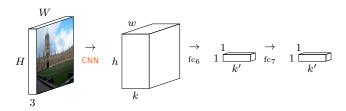
- query images
- nearest neighbors in ImageNet according to Euclidean distance



- 3-channel RGB input,  $224 \times 224$
- AlexNet last pooling layer, global descriptor of dimension  $w \times h \times k = 6 \times 6 \times 256 = 9216$
- alternatively: fully connected layers  $fc_6$ ,  $fc_7$ , global descriptors of dimension k' = 4096 (best is  $fc_6$ )
- in each case: PCA-whitening,  $\ell_2$  normalization

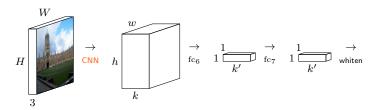


- 3-channel RGB input,  $224 \times 224$
- AlexNet last pooling layer, global descriptor of dimension  $w \times h \times k = 6 \times 6 \times 256 = 9216$
- alternatively: fully connected layers  $fc_6$ ,  $fc_7$ , global descriptors of dimension k' = 4096 (best is  $fc_6$ )
- in each case: PCA-whitening,  $\ell_2$  normalization



- 3-channel RGB input,  $224 \times 224$
- AlexNet last pooling layer, global descriptor of dimension  $w \times h \times k = 6 \times 6 \times 256 = 9216$
- alternatively: fully connected layers  $fc_6$ ,  $fc_7$ , global descriptors of dimension k' = 4096 (best is  $fc_6$ )
- in each case: PCA-whitening,  $\ell_2$  normalization





- 3-channel RGB input,  $224 \times 224$
- AlexNet last pooling layer, global descriptor of dimension  $w \times h \times k = 6 \times 6 \times 256 = 9216$
- alternatively: fully connected layers  $fc_6$ ,  $fc_7$ , global descriptors of dimension k' = 4096 (best is  $fc_6$ )
- in each case: PCA-whitening,  $\ell_2$  normalization





- fine-tuning by softmax on 672 classes of 200 k landmark photos
- outperforms VLAD and Fisher vectors on standard retrieval benchmarks, but still inferior to SIFT local descriptors

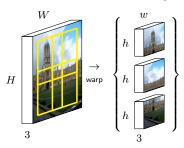




- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into  $w \times h = 227 \times 227$
- each region yields a  $w' \times h' \times k = 36 \times 36 \times 256$  dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening of each descriptor

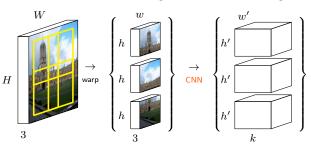


- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into  $w \times h = 227 \times 227$
- each region yields a  $w' \times h' \times k = 36 \times 36 \times 256$  dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening of each descriptor



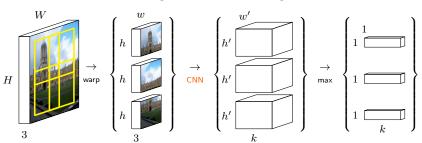
- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into w imes h = 227 imes 227
- each region yields a  $w' \times h' \times k = 36 \times 36 \times 256$  dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening of each descriptor





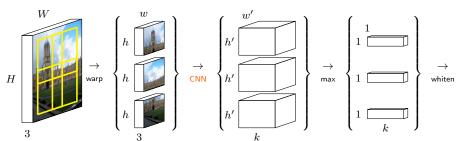
- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into  $w \times h = 227 \times 227$
- each region yields a  $w' \times h' \times k = 36 \times 36 \times 256$  dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening of each descriptor



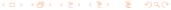


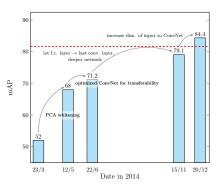
- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into  $w \times h = 227 \times 227$
- each region yields a  $w' \times h' \times k = 36 \times 36 \times 256$  dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening of each descriptor



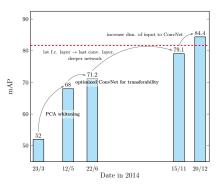


- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into w imes h = 227 imes 227
- each region yields a  $w' \times h' \times k = 36 \times 36 \times 256$  dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening of each descriptor





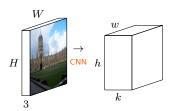
- CNN visual representation jumps by more than 30% mAP to outperform standard SIFT pipeline in a few months
- however, this is based on multiple regional descriptors per image and exhaustive pairwise matching of all descriptors of query and all dataset images, which is not practical



- $\bullet$  CNN visual representation jumps by more than 30% mAP to outperform standard SIFT pipeline in a few months
- however, this is based on multiple regional descriptors per image and exhaustive pairwise matching of all descriptors of query and all dataset images, which is not practical

## regional max-pooling (R-MAC)

[Tolias et al. 2016]

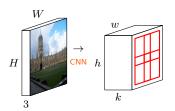


- VGG-16 last convolutional layer, k=512
- fixed multiscale overlapping regions, spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- sum-pooling over all descriptors,  $\ell_2$ -normalization



# regional max-pooling (R-MAC)

[Tolias et al. 2016]

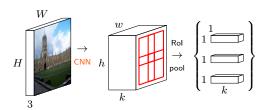


- VGG-16 last convolutional layer, k=512
- fixed multiscale overlapping regions, spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- sum-pooling over all descriptors,  $\ell_2$ -normalization



### regional max-pooling (R-MAC)

[Tolias et al. 2016]

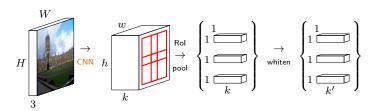


- VGG-16 last convolutional layer, k = 512
- fixed multiscale overlapping regions, spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- sum-pooling over all descriptors,  $\ell_2$ -normalization



#### regional max-pooling (R-MAC)

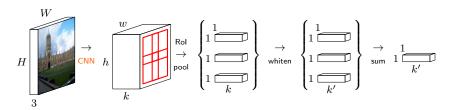
[Tolias et al. 2016]



- VGG-16 last convolutional layer, k = 512
- fixed multiscale overlapping regions, spatial max-pooling
- ullet  $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- ullet sum-pooling over all descriptors,  $\ell_2$ -normalization

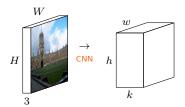
#### regional max-pooling (R-MAC)

[Tolias et al. 2016]



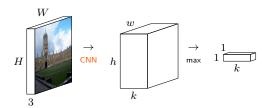
- VGG-16 last convolutional layer, k = 512
- fixed multiscale overlapping regions, spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- sum-pooling over all descriptors,  $\ell_2$ -normalization

# global max-pooling (MAC)



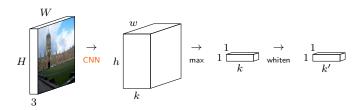
- VGG-16 last convolutional layer, k = 512
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- MAC: maximum activation of convolutions

# global max-pooling (MAC)



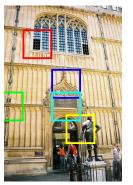
- VGG-16 last convolutional layer, k = 512
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- MAC: maximum activation of convolutions

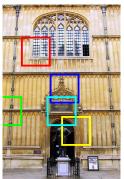
### global max-pooling (MAC)



- VGG-16 last convolutional layer, k = 512
- global spatial max-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- MAC: maximum activation of convolutions

#### global max-pooling: matching

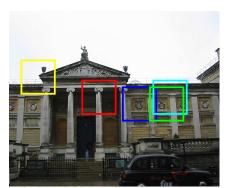


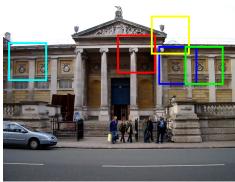


 receptive fields of 5 components of MAC vectors that contribute most to image similarity



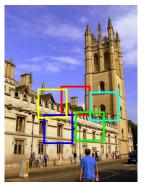
#### global max-pooling: matching

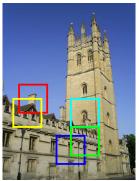




 receptive fields of 5 components of MAC vectors that contribute most to image similarity

#### global max-pooling: matching

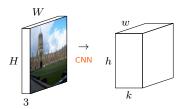




 receptive fields of 5 components of MAC vectors that contribute most to image similarity

# global sum-pooling (SPoC)\*

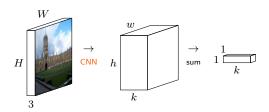
[Babenko and Lempitsky 2015]



- VGG-19 last convolutional layer, k = 512
- global spatial sum-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- SPoC: sum-pooled convolutional features

# global sum-pooling (SPoC)\*

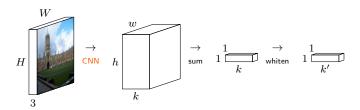
[Babenko and Lempitsky 2015]



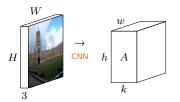
- VGG-19 last convolutional layer, k = 512
- global spatial sum-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- SPoC: sum-pooled convolutional features

# global sum-pooling (SPoC)\*

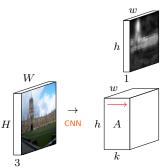
[Babenko and Lempitsky 2015]



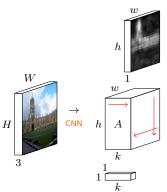
- VGG-19 last convolutional layer, k = 512
- global spatial sum-pooling
- $\ell_2$ -normalization, PCA-whitening,  $\ell_2$ -normalization
- SPoC: sum-pooled convolutional features



- VGG-16 feature map A, last pooling layer, k = 512

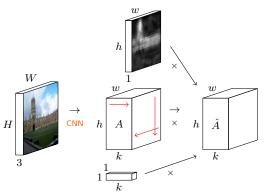


- VGG-16 feature map A, last pooling layer, k = 512
- spatial weights F, channel weights w, weighted feature map



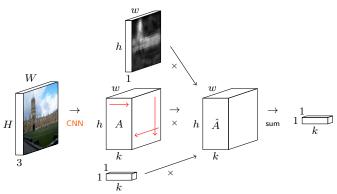
- VGG-16 feature map A, last pooling layer, k = 512
- spatial weights F, channel weights  $\mathbf{w}$ , weighted feature map

[Kalantidis et al. 2016]

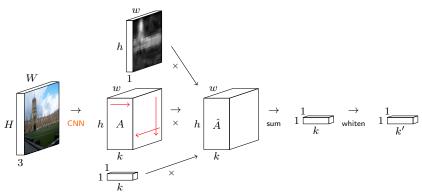


- VGG-16 feature map A, last pooling layer, k = 512
- spatial weights F, channel weights  $\mathbf{w}$ , weighted feature map

Kalantidis, Mellina, Osindero. ECCVW 2016. Cross-Dimensional Weighting for Aggregated Deep Convolutional Features.



- VGG-16 feature map A, last pooling layer, k = 512
- spatial weights F, channel weights  $\mathbf{w}$ , weighted feature map
- global spatial sum-pooling



- VGG-16 feature map A, last pooling layer, k=512
- ullet spatial weights F, channel weights old w, weighted feature map
- global spatial sum-pooling
- $\ell_p$ -normalization, PCA-whitening,  $\ell_2$ -normalization



• spatial weights (visual saliency)

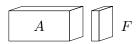
$$F(x,y) = \sum_{k} A_k(x,y)$$

channel weights (sparsity sensitive)

$$w_j = -\log\left(\epsilon + \sum_{x,y} \mathbb{1}[A_j(x,y)]\right)$$

$$\hat{A} = A \times F \times \mathbf{w}$$





spatial weights (visual saliency)

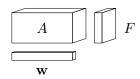
$$F(x,y) = \sum_{k} A_k(x,y)$$

channel weights (sparsity sensitive)

$$w_j = -\log\left(\epsilon + \sum_{x,y} \mathbb{1}[A_j(x,y)]\right)$$

$$\hat{A} = A \times F \times \mathbf{w}$$





• spatial weights (visual saliency)

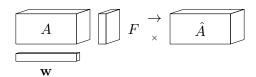
$$F(x,y) = \sum_{k} A_k(x,y)$$

channel weights (sparsity sensitive)

$$w_j = -\log\left(\epsilon + \sum_{x,y} \mathbb{1}[A_j(x,y)]\right)$$

$$\hat{A} = A \times F \times \mathbf{w}$$





spatial weights (visual saliency)

$$F(x,y) = \sum_{k} A_k(x,y)$$

channel weights (sparsity sensitive)

$$w_j = -\log\left(\epsilon + \sum_{x,y} \mathbb{1}[A_j(x,y)]\right)$$

$$\hat{A} = A \times F \times \mathbf{w}$$









• input image







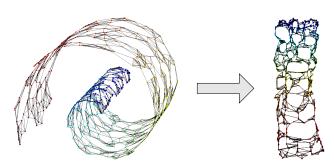


• receptive fields of nonzero elements of the 10 channels with the highest sparsity-sensitive weights

Kalantidis, Mellina, Osindero. ECCVW 2016. Cross-Dimensional Weighting for Aggregated Deep Convolutional Features.

# manifold learning

#### manifold learning



- e.g. Isomap: apply PCA to the geodesic (graph) distance matrix
- e.g. kernel PCA: apply PCA to the Gram matrix of a nonlinear kernel
- other topology-preserving methods are only focusing on distances to nearest neighbors
- many classic methods use eigenvalue decomposition and most do not learn and explicit mapping from the input to the embedding space

#### siamese architecture

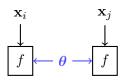
[Chopra et al. 2005]

 $\mathbf{x}_i$   $\mathbf{x}_j$ 

- an input sample is a pair  $(\mathbf{x}_i, \mathbf{x}_j)$
- ullet both  $\mathbf{x}_i, \mathbf{x}_j$  go through the same function f with shared parameters heta
- ullet loss  $\ell_{ij}$  is measured on output pair  $(\mathbf{y}_i,\mathbf{y}_j)$  and target  $t_{ij}$

#### siamese architecture

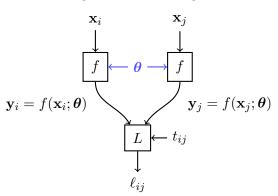
[Chopra et al. 2005]



- an input sample is a pair  $(\mathbf{x}_i, \mathbf{x}_j)$
- ullet both  $\mathbf{x}_i, \mathbf{x}_j$  go through the same function f with shared parameters  $oldsymbol{ heta}$
- ullet loss  $\ell_{ij}$  is measured on output pair  $(\mathbf{y}_i,\mathbf{y}_j)$  and target  $t_{ij}$

#### siamese architecture

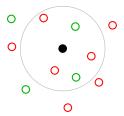
[Chopra et al. 2005]



- an input sample is a pair  $(\mathbf{x}_i, \mathbf{x}_j)$
- ullet both  $\mathbf{x}_i, \mathbf{x}_j$  go through the same function f with shared parameters  $oldsymbol{ heta}$
- ullet loss  $\ell_{ij}$  is measured on output pair  $(\mathbf{y}_i,\mathbf{y}_j)$  and target  $t_{ij}$

#### contrastive loss

[Hadsel et al. 2006]



- input samples  $\mathbf{x}_i$ , output vectors  $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- ullet target variables  $t_{ij} = \mathbb{1}[\sin(\mathbf{x}_i,\mathbf{x}_j)]$
- contrastive loss is a function of distance  $\|\mathbf{y}_i \mathbf{y}_j\|$  only

$$\ell_{ij} = L((\mathbf{y}_i, \mathbf{y}_j), t_{ij}) = \ell(\|\mathbf{y}_i - \mathbf{y}_j\|, t_{ij})$$

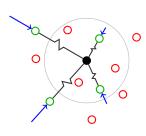
similar samples are attracted

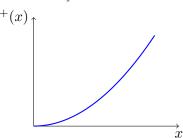
$$\ell(x,t) = t\ell^{+}(x) + (1-t)\ell^{-}(x) = tx^{2} + (1-t)[m-x]_{+}^{2}$$



#### contrastive loss

[Hadsel et al. 2006]





- input samples  $\mathbf{x}_i$ , output vectors  $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- target variables  $t_{ij} = \mathbb{1}[\sin(\mathbf{x}_i, \mathbf{x}_j)]$
- contrastive loss is a function of distance  $\|\mathbf{y}_i \mathbf{y}_j\|$  only

$$\ell_{ij} = L((\mathbf{y}_i, \mathbf{y}_j), t_{ij}) = \ell(\|\mathbf{y}_i - \mathbf{y}_j\|, t_{ij})$$

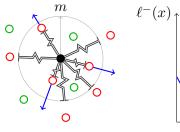
similar samples are attracted

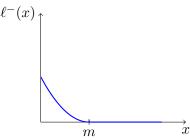
$$\ell(x,t) = t\ell^+(x) + (1-t)\ell^-(x) = tx^2 + (1-t)[m-x]_+^2$$



#### contrastive loss

[Hadsel et al. 2006]





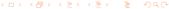
- input samples  $\mathbf{x}_i$ , output vectors  $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- ullet target variables  $t_{ij} = \mathbb{1}[\mathrm{sim}(\mathbf{x}_i,\mathbf{x}_j)]$
- contrastive loss is a function of distance  $\|\mathbf{y}_i \mathbf{y}_j\|$  only

$$\ell_{ij} = L((\mathbf{y}_i, \mathbf{y}_j), t_{ij}) = \ell(\|\mathbf{y}_i - \mathbf{y}_j\|, t_{ij})$$

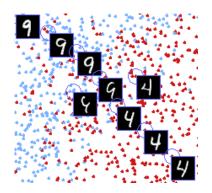
ullet dissimilar samples are repelled if closer than margin m

$$\ell(x,t) = t\ell^{+}(x) + (1-t)\ell^{-}(x) = tx^{2} + (1-t)[m-x]_{+}^{2}$$





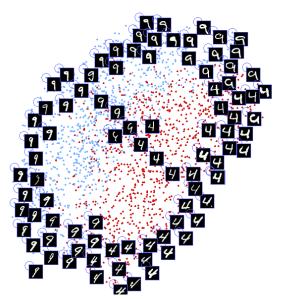
#### manifold learning: MNIST



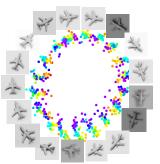
- 3k samples of each of digits 4,9
- each sample similar to its 5 Euclidean nearest neighbors, and dissimilar to all other points
- 30k similar pairs, 18M dissimilar pairs



#### manifold learning: MNIST

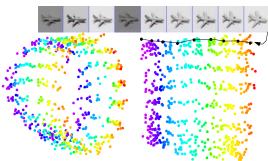


#### manifold learning: NORB



- 972 images of airplane class: 18 azimuths (every  $20^\circ$ ), 9 elevations (in  $[30^\circ,70^\circ]$ , every  $5^\circ$ ), 6 lighting conditions
- samples similar if taken from contiguous azimuth or elevation, regardless of lighting
- 11k similar pairs, 206M dissimilar pairs
- cylindrer in 3d: azimuth on circumference, elevation on height

#### manifold learning: NORB



- 972 images of airplane class: 18 azimuths (every  $20^\circ$ ), 9 elevations (in  $[30^\circ,70^\circ]$ , every  $5^\circ$ ), 6 lighting conditions
- samples similar if taken from contiguous azimuth or elevation, regardless of lighting
- 11k similar pairs, 206M dissimilar pairs
- cylindrer in 3d: azimuth on circumference, elevation on height

#### triplet architecture

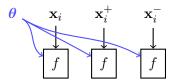
[Wang et al. 2014]

$$\mathbf{x}_i \qquad \mathbf{x}_i^+ \qquad \mathbf{x}_i^-$$

- ullet an input sample is a triplet  $(\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-)$
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through the same function f with shared parameters heta
- ullet loss  $\ell_i$  measured on output triplet  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

#### triplet architecture

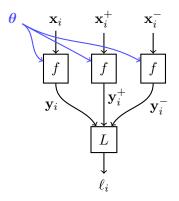
[Wang et al. 2014]



- ullet an input sample is a triplet  $(\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-)$
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through the same function f with shared parameters  $oldsymbol{ heta}$
- ullet loss  $\ell_i$  measured on output triplet  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

#### triplet architecture

[Wang et al. 2014]



- ullet an input sample is a triplet  $(\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-)$
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through the same function f with shared parameters  $oldsymbol{ heta}$
- ullet loss  $\ell_i$  measured on output triplet  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$



#### triplet loss

- input "anchor"  $\mathbf{x}_i$ , output vector  $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- positive  $\mathbf{y}_i^+ = f(\mathbf{x}_i^+; \boldsymbol{\theta})$ , negative  $\mathbf{y}_i^- = f(\mathbf{x}_i^-; \boldsymbol{\theta})$
- triplet loss is a function of distances  $\|\mathbf{y}_i \mathbf{y}_i^+\|, \|\mathbf{y}_i \mathbf{y}_i^-\|$  only

$$\ell_i = L(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-) = \ell(\|\mathbf{y}_i - \mathbf{y}_i^+\|, \|\mathbf{y}_i - \mathbf{y}_i^-\|)$$
$$\ell(x^+, x^-) = [m + (x^+)^2 - (x^-)^2]$$

so distance  $\|\mathbf{y}_i - \mathbf{y}_i^+\|$  should be less than  $\|\mathbf{y}_i - \mathbf{y}_i^-\|$  by margin m

• by taking two pairs  $(\mathbf{x}_i, \mathbf{x}_i^+)$  and  $(\mathbf{x}_i, \mathbf{x}_i^-)$  at a time with targets 1, 0 respectively, the contrastive loss can be written similarly

$$\ell(x^+, x^-) = (x^+)^2 + [m - x^-]_+^2$$

so distance  $\|\mathbf{y}_i - \mathbf{y}_i^+\|$  should small and  $\|\mathbf{y}_i - \mathbf{y}_i^-\|$  larger than m



#### triplet loss

- input "anchor"  $\mathbf{x}_i$ , output vector  $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- positive  $\mathbf{y}_i^+ = f(\mathbf{x}_i^+; m{ heta})$ , negative  $\mathbf{y}_i^- = f(\mathbf{x}_i^-; m{ heta})$
- triplet loss is a function of distances  $\|\mathbf{y}_i \mathbf{y}_i^+\|, \|\mathbf{y}_i \mathbf{y}_i^-\|$  only

$$\ell_i = L(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-) = \ell(\|\mathbf{y}_i - \mathbf{y}_i^+\|, \|\mathbf{y}_i - \mathbf{y}_i^-\|)$$
$$\ell(x^+, x^-) = [m + (x^+)^2 - (x^-)^2]$$

so distance  $\|\mathbf{y}_i - \mathbf{y}_i^+\|$  should be less than  $\|\mathbf{y}_i - \mathbf{y}_i^-\|$  by margin m

• by taking two pairs  $(\mathbf{x}_i, \mathbf{x}_i^+)$  and  $(\mathbf{x}_i, \mathbf{x}_i^-)$  at a time with targets 1, 0 respectively, the contrastive loss can be written similarly

$$\ell(x^+, x^-) = (x^+)^2 + [m - x^-]_+^2$$

so distance  $\|\mathbf{y}_i - \mathbf{y}_i^+\|$  should small and  $\|\mathbf{y}_i - \mathbf{y}_i^-\|$  larger than m



# unsupervised learning by context prediction

[Doersch et al. 2015]

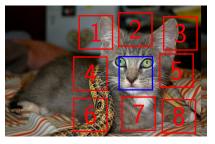


- sample random pairs of patches in one of eight spatial configurations
- patches are randomly jittered and do not overlap
- like solving a puzzle, learn to predict the relative position

$$f\left(\begin{array}{cc} \end{array}\right) = 3$$

## unsupervised learning by context prediction

[Doersch et al. 2015]

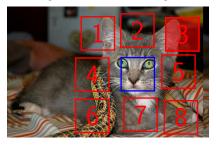


- sample random pairs of patches in one of eight spatial configurations
- patches are randomly jittered and do not overlap
- like solving a puzzle, learn to predict the relative position

$$f\left(\begin{array}{cc} \end{array}\right) = 3$$

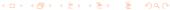
## unsupervised learning by context prediction

[Doersch et al. 2015]

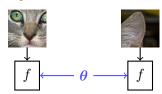


- sample random pairs of patches in one of eight spatial configurations
- patches are randomly jittered and do not overlap
- like solving a puzzle, learn to predict the relative position

$$f\left(\begin{array}{c} \bullet \\ \bullet \\ \bullet \end{array}\right) = 3$$

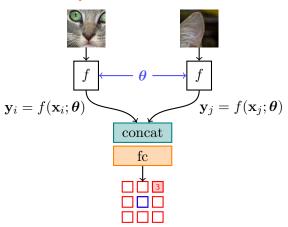


#### context prediction: architecture



- network f learned by siamese architecture
- representations are concatenated and followed by softmax classifier, where each spatial configuration is a class

#### context prediction: architecture



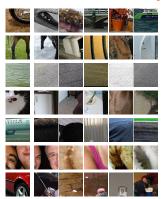
network f learned by siamese architecture

Doersch, Gupta, Efros. ICCV 2015. Unsupervised Visual Representation Learning By Context Prediction.

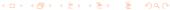
 representations are concatenated and followed by softmax classifier, where each spatial configuration is a class

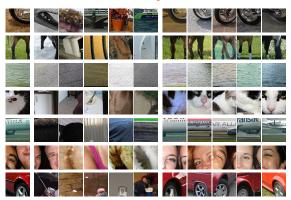


- input image
- nearest neighbors with randomly initialized network
- trained by supervised classification on ImageNet
- unsupervised training from scratch on the context prediction task

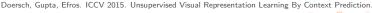


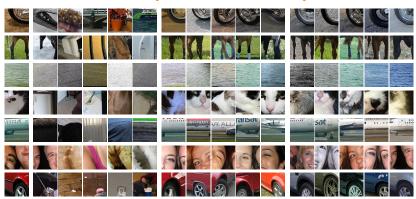
- input image
- nearest neighbors with randomly initialized network
- trained by supervised classification on ImageNet
- unsupervised training from scratch on the context prediction task





- input image
- nearest neighbors with randomly initialized network
- trained by supervised classification on ImageNet
- unsupervised training from scratch on the context prediction task





- input image
- nearest neighbors with randomly initialized network
- trained by supervised classification on ImageNet
- unsupervised training from scratch on the context prediction task

# unsupervised learning on video: tracking

[Wang et al. 2015]

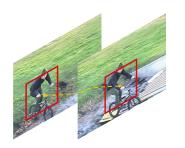


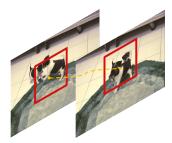


- estimate motion and find the region that contains most motion
- track this region for a number of frames
- generate a pair of matching patches on the first and last frames

# unsupervised learning on video: tracking

[Wang et al. 2015]

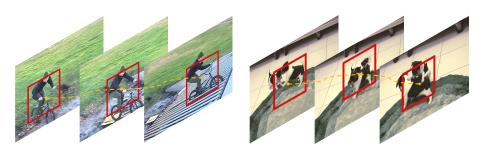




- estimate motion and find the region that contains most motion
- track this region for a number of frames
- generate a pair of matching patches on the first and last frames

## unsupervised learning on video: tracking

[Wang et al. 2015]



- estimate motion and find the region that contains most motion
- track this region for a number of frames
- generate a pair of matching patches on the first and last frames

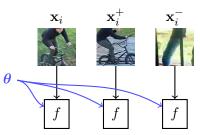




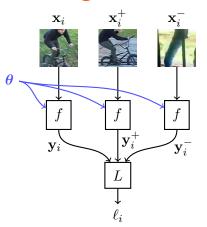


- ullet input query  $\mathbf{x}_i$  (first frame), tracked  $\mathbf{x}_i^+$  (last frame), random  $\mathbf{x}_i^-$
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through the same function f with shared parameters  $m{ heta}$
- triplet loss  $\ell_i$  measured on output triplet  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$



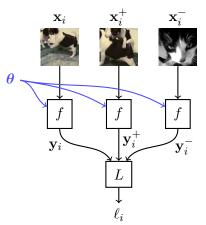


- ullet input query  $\mathbf{x}_i$  (first frame), tracked  $\mathbf{x}_i^+$  (last frame), random  $\mathbf{x}_i^-$
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through the same function f with shared parameters  $oldsymbol{ heta}$
- triplet loss  $\ell_i$  measured on output triplet  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$



- ullet input query  $\mathbf{x}_i$  (first frame), tracked  $\mathbf{x}_i^+$  (last frame), random  $\mathbf{x}_i^-$
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through the same function f with shared parameters  $oldsymbol{ heta}$
- triplet loss  $\ell_i$  measured on output triplet  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$





- ullet input query  $\mathbf{x}_i$  (first frame), tracked  $\mathbf{x}_i^+$  (last frame), random  $\mathbf{x}_i^-$
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through the same function f with shared parameters  $oldsymbol{ heta}$
- triplet loss  $\ell_i$  measured on output triplet  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$



## unsupervised learning on video: objective

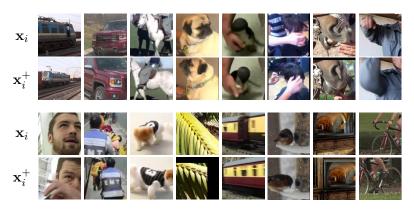
$$\left\| f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) - f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) \right\|^{2} < \left\| f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) - f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) \right\|^{2} - m$$

$$\left\| f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) - f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) \right\|^{2} < \left\| f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) - f\left( \begin{array}{c} \bullet \\ \bullet \end{array} \right) \right\|^{2} - m$$

• so, the objective is that squared distance  $\|\mathbf{y}_i - \mathbf{y}_i^+\|^2$  is less than  $\|\mathbf{y}_i - \mathbf{y}_i^-\|^2$  by margin m



## unsupervised learning on video: more examples



• input query  $\mathbf{x}_i$  (first frame), tracked  $\mathbf{x}_i^+$  (last frame)

Wang and Gupta. ICCV 2015. Unsupervised Learning of Visual Representations Using Videos.



# fine-tuning

# deep image retrieval: dataset cleaning

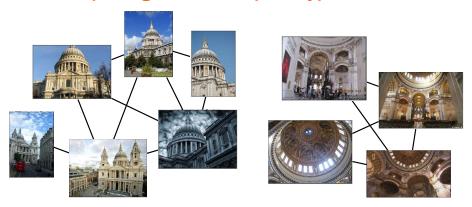
[Gordo et al. 2016]



- start from landmark dataset (192k images) and clean it (49k images)
- use it to fine-tune a network pre-trained on ImageNet for classification
- prototypical, non-prototypical and incorrect images per class
- only prototypical are kept to reduce intra-class variability

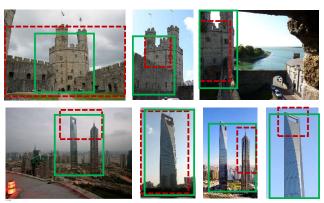


## deep image retrieval: prototypical views

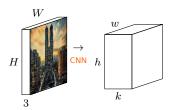


- pairwise match images per class by SIFT descriptors and fast spatial matching
- connect images into a graph and compute the connected components
- keep only the largest component

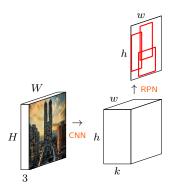
## deep image retrieval: bounding boxes



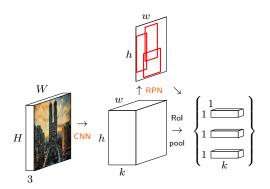
- automatically find object bounding boxes
  - initialize with inlier features per image
  - update such that boxes are consistent over all matching pairs
- use bounding boxes to train a region proposal network



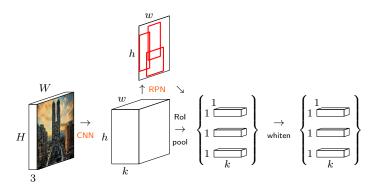
- VGG-16 or ResNet-101 feature maps
- proposals detected on feature maps by RPN and max-pooled
- $\ell_2$ -normalization, PCA-whitening (FC layer),  $\ell_2$ -normalization
- sum-pooling,  $\ell_2$ -normalization (as in R-MAC)



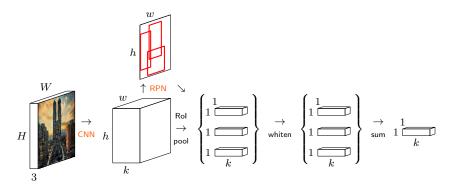
- VGG-16 or ResNet-101 feature maps
- proposals detected on feature maps by RPN and max-pooled
- ullet  $\ell_2$ -normalization, PCA-whitening (FC layer),  $\ell_2$ -normalization
- sum-pooling,  $\ell_2$ -normalization (as in R-MAC)



- VGG-16 or ResNet-101 feature maps
- proposals detected on feature maps by RPN and max-pooled
- ullet  $\ell_2$ -normalization, PCA-whitening (FC layer),  $\ell_2$ -normalization
- sum-pooling,  $\ell_2$ -normalization (as in R-MAC)



- VGG-16 or ResNet-101 feature maps
- proposals detected on feature maps by RPN and max-pooled
- $\ell_2$ -normalization, PCA-whitening (FC layer),  $\ell_2$ -normalization
- sum-pooling,  $\ell_2$ -normalization (as in R-MAC)



- VGG-16 or ResNet-101 feature maps
- proposals detected on feature maps by RPN and max-pooled
- ullet  $\ell_2$ -normalization, PCA-whitening (FC layer),  $\ell_2$ -normalization
- sum-pooling,  $\ell_2$ -normalization (as in R-MAC)



## deep image retrieval: architecture

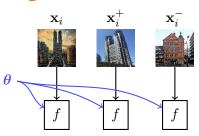






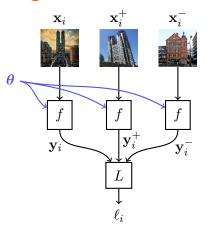
- ullet query  $\mathbf{x}_i$ , relevant  $\mathbf{x}_i^+$  (same building), irrelevant  $\mathbf{x}_i^-$  (other building)
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through function f including features, RPN, pooling
- ullet triplet loss  $\ell_i$  measured on output  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

## deep image retrieval: architecture



- query  $\mathbf{x}_i$ , relevant  $\mathbf{x}_i^+$  (same building), irrelevant  $\mathbf{x}_i^-$  (other building)
- ullet  $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through function f including features, RPN, pooling
- ullet triplet loss  $\ell_i$  measured on output  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

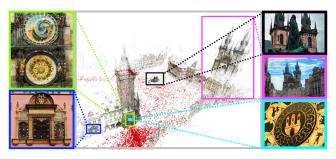
## deep image retrieval: architecture



- query  $\mathbf{x}_i$ , relevant  $\mathbf{x}_i^+$  (same building), irrelevant  $\mathbf{x}_i^-$  (other building)
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$  go through function f including features, RPN, pooling
- triplet loss  $\ell_i$  measured on output  $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

## learning from bag-of-words: 3d reconstruction

[Radenovic et al. 2016]



- start from an independent dataset of 7.4M images, no class labels
- clustering, pairwise matching and reconstruction of 713~3d models containing 165k unique images
- 3d models playing the same role as classes in deep image retrieval
- again, fine-tune a network pre-trained on ImageNet for classification













 positive images found in same model by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)



- input query
- positive images found in same model by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)



- input query
- positive images found in same model by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)



- input query
- positive images found in same model by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)



- input query
- negative images found in different models
- hard negatives are most similar to query, i.e. with minimum MAC distance
- hardest negative, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)



- input query
- negative images found in different models
- hard negatives are most similar to query, i.e. with minimum MAC distance
- hardest negative, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)



- input query
- negative images found in different models
- hard negatives are most similar to query, i.e. with minimum MAC distance
- hardest negative, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)



- input query
- negative images found in different models
- hard negatives are most similar to query, i.e. with minimum MAC distance
- hardest negative, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)

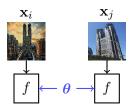
#### learning from bag-of-words: architecture





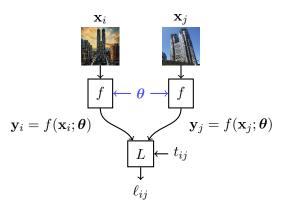
- input  $(\mathbf{x}_i, \mathbf{x}_j)$  of relevant or irrelevant images
- ullet both  $\mathbf{x}_i, \mathbf{x}_j$  go through function f including features and MAC pooling
- ullet contrastive loss  $\ell_{ij}$  measured on output  $(\mathbf{y}_i,\mathbf{y}_j)$  and target  $t_{ij}$

#### learning from bag-of-words: architecture



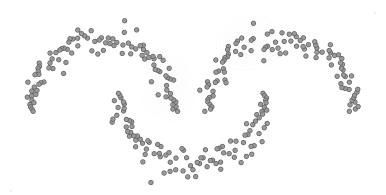
- input  $(\mathbf{x}_i, \mathbf{x}_j)$  of relevant or irrelevant images
- ullet both  ${f x}_i,{f x}_j$  go through function f including features and MAC pooling
- ullet contrastive loss  $\ell_{ij}$  measured on output  $(\mathbf{y}_i,\mathbf{y}_j)$  and target  $t_{ij}$

#### learning from bag-of-words: architecture

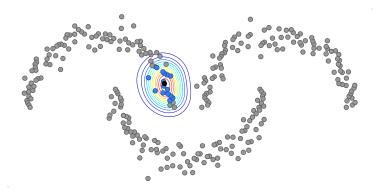


- input  $(\mathbf{x}_i, \mathbf{x}_j)$  of relevant or irrelevant images
- ullet both  $\mathbf{x}_i, \mathbf{x}_j$  go through function f including features and MAC pooling
- ullet contrastive loss  $\ell_{ij}$  measured on output  $(\mathbf{y}_i,\mathbf{y}_j)$  and target  $t_{ij}$

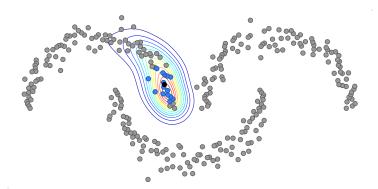
# graph-based methods



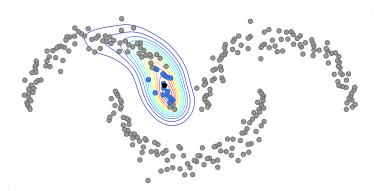
- data points (•), query point (•), nearest neighbors (•)
- iteration  $\times$  30



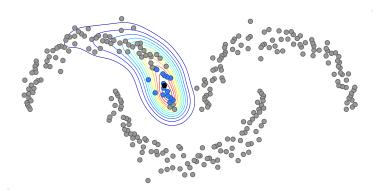
- data points (•), query point (•), nearest neighbors (•)
- iteration  $0 \times 30$



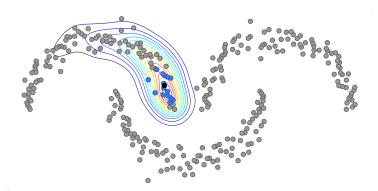
- data points (•), query point (•), nearest neighbors (•)
- iteration  $1 \times 30$



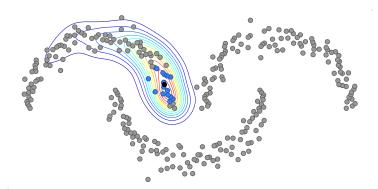
- data points (•), query point (•), nearest neighbors (•)
- iteration  $2 \times 30$



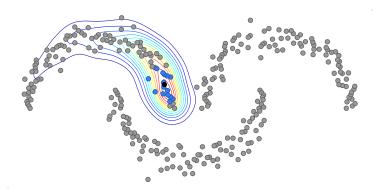
- data points (•), query point (•), nearest neighbors (•)
- iteration  $3 \times 30$



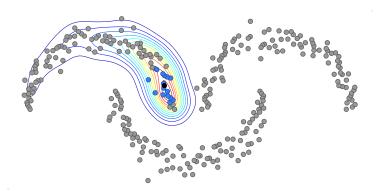
- data points (•), query point (•), nearest neighbors (•)
- iteration  $4 \times 30$



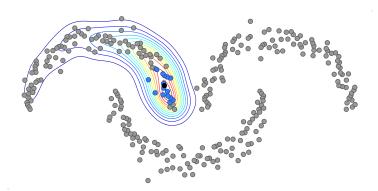
- data points (•), query point (•), nearest neighbors (•)
- iteration  $5 \times 30$



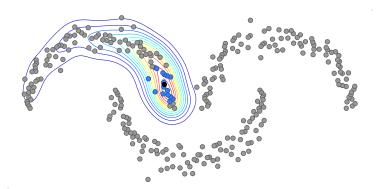
- data points (•), query point (•), nearest neighbors (•)
- iteration  $6 \times 30$



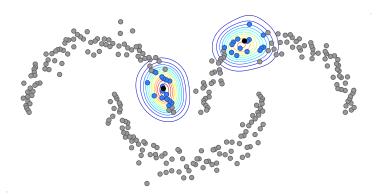
- data points (•), query point (•), nearest neighbors (•)
- iteration  $7 \times 30$



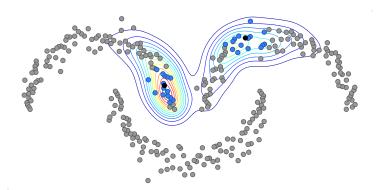
- data points (•), query point (•), nearest neighbors (•)
- iteration  $8 \times 30$



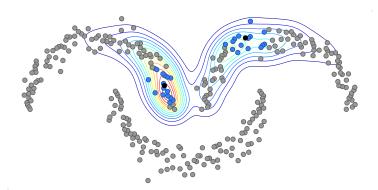
- data points (•), query point (•), nearest neighbors (•)
- iteration  $9 \times 30$



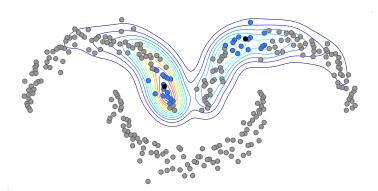
- data points (•), query points (•), nearest neighbors (•)
- iteration  $0 \times 30$



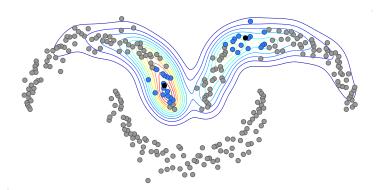
- data points (•), query points (•), nearest neighbors (•)
- iteration  $1 \times 30$



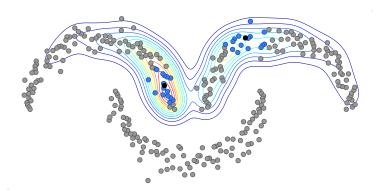
- data points (•), query points (•), nearest neighbors (•)
- iteration  $2 \times 30$



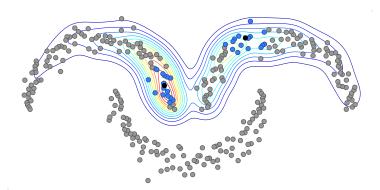
- data points (•), query points (•), nearest neighbors (•)
- iteration  $3 \times 30$



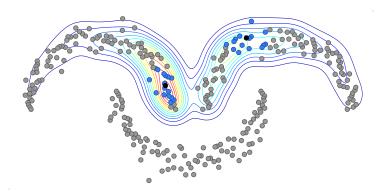
- data points (•), query points (•), nearest neighbors (•)
- iteration  $4 \times 30$



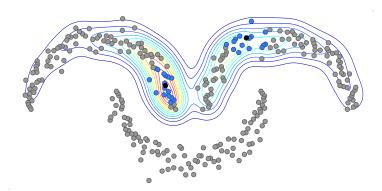
- data points (•), query points (•), nearest neighbors (•)
- iteration  $5 \times 30$



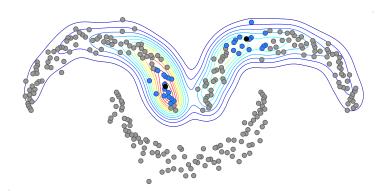
- data points (•), query points (•), nearest neighbors (•)
- iteration  $6 \times 30$



- data points (•), query points (•), nearest neighbors (•)
- iteration  $7 \times 30$



- data points (•), query points (•), nearest neighbors (•)
- iteration  $8 \times 30$



- data points (•), query points (•), nearest neighbors (•)
- iteration  $9 \times 30$

# ranking on manifolds: random walk

[Zhou et al. 2003]

- ullet reciprocal nearest neighbor graph on n data points
- non-negative, symmetric, sparse adjacency matrix  $W \in \mathbb{R}^{n \times n}$ , with zero diagonal (no self-loops)
- symmetrically normalized adjacency matrix

$$W := D^{-1/2} W D^{-1/2}$$

where D = diag(W1) is the degree matrix

- query: vector  $\mathbf{y} \in \mathbb{R}^n$  with  $y_i = \mathbb{1}[i \text{ is query}]$
- random walk: starting with any  $\mathbf{f}^{(0)} \in \mathbb{R}^n$ , iterate

$$\mathbf{f}^{(\tau)} = \alpha \mathcal{W} \mathbf{f}^{(\tau-1)} + (1 - \alpha) \mathbf{y}$$

where  $\alpha \in [0,1)$  (typically close to 1)

rank data points by descending order of f



# ranking on manifolds: random walk

[Zhou et al. 2003]

- ullet reciprocal nearest neighbor graph on n data points
- non-negative, symmetric, sparse adjacency matrix  $W \in \mathbb{R}^{n \times n}$ , with zero diagonal (no self-loops)
- symmetrically normalized adjacency matrix

$$W := D^{-1/2}WD^{-1/2}$$

where D = diag(W1) is the degree matrix

- query: vector  $\mathbf{y} \in \mathbb{R}^n$  with  $y_i = \mathbb{1}[i \text{ is query}]$
- random walk: starting with any  $\mathbf{f}^{(0)} \in \mathbb{R}^n$ , iterate

$$\mathbf{f}^{(\tau)} = \alpha \mathcal{W} \mathbf{f}^{(\tau-1)} + (1 - \alpha) \mathbf{y}$$

where  $\alpha \in [0,1)$  (typically close to 1)

rank data points by descending order of f



# ranking on manifolds: random walk

[Zhou et al. 2003]

- ullet reciprocal nearest neighbor graph on n data points
- non-negative, symmetric, sparse adjacency matrix  $W \in \mathbb{R}^{n \times n}$ , with zero diagonal (no self-loops)
- symmetrically normalized adjacency matrix

$$W := D^{-1/2}WD^{-1/2}$$

where D = diag(W1) is the degree matrix

- query: vector  $\mathbf{y} \in \mathbb{R}^n$  with  $y_i = \mathbb{1}[i \text{ is query}]$
- random walk: starting with any  $\mathbf{f}^{(0)} \in \mathbb{R}^n$ , iterate

$$\mathbf{f}^{(\tau)} = \alpha \mathcal{W} \mathbf{f}^{(\tau-1)} + (1 - \alpha) \mathbf{y}$$

where  $\alpha \in [0,1)$  (typically close to 1)

rank data points by descending order of f



# ranking on manifolds: random walk

[Zhou et al. 2003]

- ullet reciprocal nearest neighbor graph on n data points
- non-negative, symmetric, sparse adjacency matrix  $W \in \mathbb{R}^{n \times n}$ , with zero diagonal (no self-loops)
- symmetrically normalized adjacency matrix

$$W := D^{-1/2}WD^{-1/2}$$

where D = diag(W1) is the degree matrix

- query: vector  $\mathbf{y} \in \mathbb{R}^n$  with  $y_i = \mathbb{1}[i \text{ is query}]$
- ullet random walk: starting with any  $\mathbf{f}^{(0)} \in \mathbb{R}^n$ , iterate

$$\mathbf{f}^{(\tau)} = \alpha \mathcal{W} \mathbf{f}^{(\tau-1)} + (1 - \alpha) \mathbf{y}$$

where  $\alpha \in [0,1)$  (typically close to 1)

rank data points by descending order of f



# ranking on manifolds: random walk

[Zhou et al. 2003]

- ullet reciprocal nearest neighbor graph on n data points
- non-negative, symmetric, sparse adjacency matrix  $W \in \mathbb{R}^{n \times n}$ , with zero diagonal (no self-loops)
- symmetrically normalized adjacency matrix

$$W := D^{-1/2}WD^{-1/2}$$

where D = diag(W1) is the degree matrix

- query: vector  $\mathbf{y} \in \mathbb{R}^n$  with  $y_i = \mathbb{1}[i \text{ is query}]$
- ullet random walk: starting with any  $\mathbf{f}^{(0)} \in \mathbb{R}^n$ , iterate

$$\mathbf{f}^{(\tau)} = \alpha \mathcal{W} \mathbf{f}^{(\tau-1)} + (1 - \alpha) \mathbf{y}$$

where  $\alpha \in [0,1)$  (typically close to 1)

rank data points by descending order of f



[Iscen et al. 2017]

ullet query: sparse vector  $\mathbf{y} \in \mathbb{R}^n$  with nearest neighbor similarities

$$y_i = \sum_{\mathbf{q} \in Q} s(\mathbf{q}, \mathbf{x}_i) \times \mathbb{1}[\mathbf{x}_i \in NN_X^k(\mathbf{q})]$$

where  $Q, X \subset \mathbb{R}^d$  query/data points,  $\mathbf{x}_i \in X$ , s similarity function

regularized Laplacian

$$\mathcal{L}_{\alpha} = \frac{I - \alpha \mathcal{W}}{1 - \alpha}$$

solve linear system

$$\mathcal{L}_{\alpha}\mathbf{f} = \mathbf{y}$$

by conjugate gradient method

[Iscen et al. 2017]

ullet query: sparse vector  $\mathbf{y} \in \mathbb{R}^n$  with nearest neighbor similarities

$$y_i = \sum_{\mathbf{q} \in Q} s(\mathbf{q}, \mathbf{x}_i) \times \mathbb{1}[\mathbf{x}_i \in NN_X^k(\mathbf{q})]$$

where  $Q, X \subset \mathbb{R}^d$  query/data points,  $\mathbf{x}_i \in X$ , s similarity function

regularized Laplacian

$$\mathcal{L}_{\alpha} = \frac{I - \alpha \mathcal{W}}{1 - \alpha}$$

solve linear system

$$\mathcal{L}_{\alpha}\mathbf{f} = \mathbf{y}$$

by conjugate gradient method

[Iscen et al. 2017]

ullet query: sparse vector  $\mathbf{y} \in \mathbb{R}^n$  with nearest neighbor similarities

$$y_i = \sum_{\mathbf{q} \in Q} s(\mathbf{q}, \mathbf{x}_i) \times \mathbb{1}[\mathbf{x}_i \in NN_X^k(\mathbf{q})]$$

where  $Q, X \subset \mathbb{R}^d$  query/data points,  $\mathbf{x}_i \in X$ , s similarity function

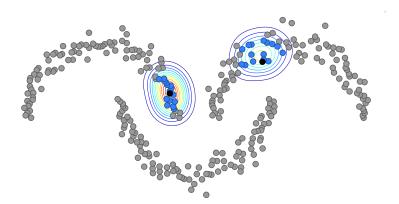
regularized Laplacian

$$\mathcal{L}_{\alpha} = \frac{I - \alpha \mathcal{W}}{1 - \alpha}$$

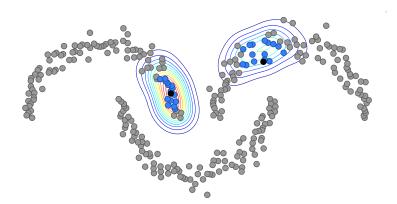
solve linear system

$$\mathcal{L}_{\alpha}\mathbf{f} = \mathbf{y}$$

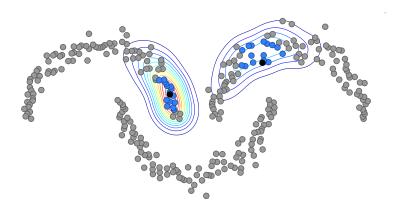
by conjugate gradient method



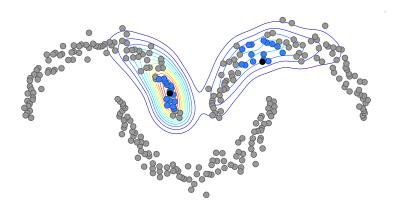
- data points (•), query points (•), nearest neighbors (•)
- iteration  $0 \times 2$



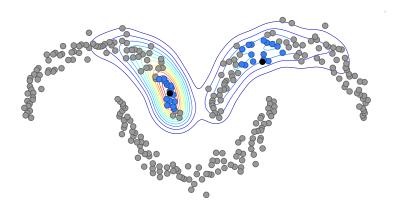
- data points (•), query points (•), nearest neighbors (•)
- iteration  $1 \times 2$



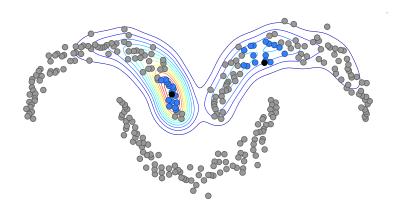
- data points (•), query points (•), nearest neighbors (•)
- iteration  $2 \times 2$



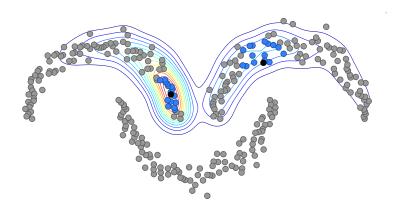
- data points (•), query points (•), nearest neighbors (•)
- iteration  $3 \times 2$



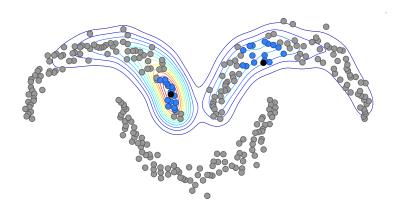
- data points (•), query points (•), nearest neighbors (•)
- iteration  $4 \times 2$



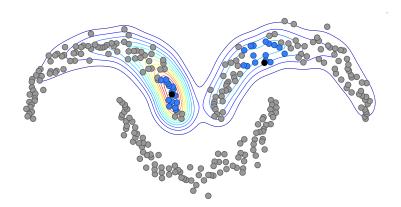
- data points (•), query points (•), nearest neighbors (•)
- iteration  $5 \times 2$



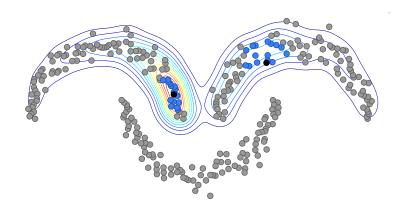
- data points (•), query points (•), nearest neighbors (•)
- iteration  $6 \times 2$



- data points (•), query points (•), nearest neighbors (•)
- iteration  $7 \times 2$



- data points (•), query points (•), nearest neighbors (•)
- iteration 8 × 2



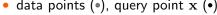
- data points (•), query points (•), nearest neighbors (•)
- iteration  $9 \times 2$

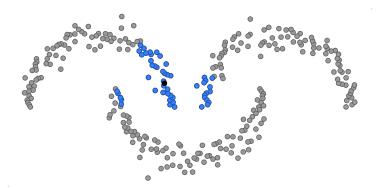
- represent image by global descriptor or multiple regional descriptors
- perform initial query based on Euclidean nearest neighbors
- re-rank by solving linear system
- ResNet-101 fine-tuned by BoW + R-MAC + re-ranking:
  - mAP 87.1 (95.8) on Oxford5k, 96.5 (96.9) on Paris6k
  - 1 (21) descriptors/image  $\times$  2048 dimensions

[Iscen et al. 2018]



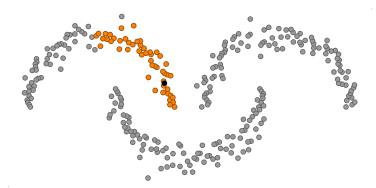
• data points (•), query point x (•)





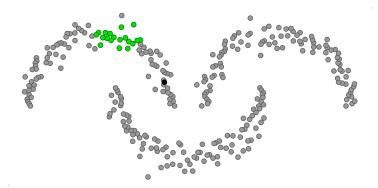
- data points (•), query point x (•)
- Euclidean nearest neighbors  $E(\mathbf{x})$  (•)





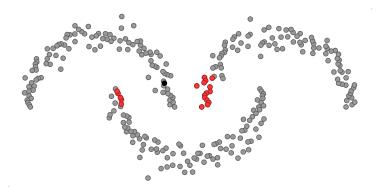
- data points (•), query point  $\mathbf{x}$  (•)
- manifold nearest neighbors  $M(\mathbf{x})$  (•)





- data points (•), query point x (•)
- hard positives  $S^+ = M(\mathbf{x}) \setminus E(\mathbf{x})$  (•)





- data points (•), query point x (•)
- hard negatives  $S^- = E(\mathbf{x}) \setminus M(\mathbf{x})$  (•)













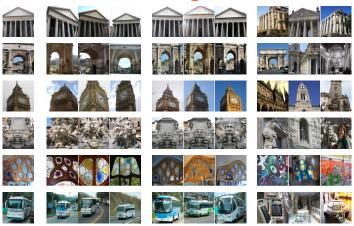
- query (anchor) (x)
- positives  $S^+(\mathbf{x})$  vs. Euclidean neighbors  $E(\mathbf{x})$
- ullet negatives  $S^-(\mathbf{x})$  vs. Euclidean non-neighbors  $X\setminus E(\mathbf{x})$



- query (anchor) (x)
- positives  $S^+(\mathbf{x})$  vs. Euclidean neighbors  $E(\mathbf{x})$
- ullet negatives  $S^-(\mathbf{x})$  vs. Euclidean non-neighbors  $X\setminus E(\mathbf{x})$



- query (anchor) (x)
- positives  $S^+(\mathbf{x})$  vs. Euclidean neighbors  $E(\mathbf{x})$
- negatives  $S^-(\mathbf{x})$  vs. Euclidean non-neighbors  $X \setminus E(\mathbf{x})$



- query (anchor) (x)
- positives  $S^+(\mathbf{x})$  vs. Euclidean neighbors  $E(\mathbf{x})$
- negatives  $S^-(\mathbf{x})$  vs. Euclidean non-neighbors  $X \setminus E(\mathbf{x})$



- query (anchor) (x)
- positives  $S^+(\mathbf{x})$  vs. Euclidean neighbors  $E(\mathbf{x})$
- negatives  $S^-(\mathbf{x})$  vs. Euclidean non-neighbors  $X \setminus E(\mathbf{x})$

- pre-train network
- extract descriptors on unlabeled dataset
- construct nearest neighbor graph
- sample anchors, measure Euclidean and manifold distances
- sample positives and negatives
- fine-tune using contrastive or triplet loss
- VGG-16 + R-MAC, mAP on Oxford5k (Paris6k):
  - pre-trained on ImageNet: 68.0 (76.6)
  - fine-tuning with SIFT + 3d reconstruction pipeline: 77.8 (84.1)
  - unsupervised fine-tuning: 78.2 (85.1)

- pre-train network
- extract descriptors on unlabeled dataset
- construct nearest neighbor graph
- sample anchors, measure Euclidean and manifold distances
- sample positives and negatives
- fine-tune using contrastive or triplet loss
- VGG-16 + R-MAC, mAP on Oxford5k (Paris6k):
  - pre-trained on ImageNet: 68.0 (76.6)
  - fine-tuning with SIFT + 3d reconstruction pipeline: 77.8 (84.1)
  - unsupervised fine-tuning: 78.2 (85.1)

- pre-train network
- extract descriptors on unlabeled dataset
- construct nearest neighbor graph
- sample anchors, measure Euclidean and manifold distances
- sample positives and negatives
- fine-tune using contrastive or triplet loss
- VGG-16 + R-MAC, mAP on Oxford5k (Paris6k):
  - pre-trained on ImageNet: 68.0 (76.6)
  - fine-tuning with SIFT + 3d reconstruction pipeline: 77.8 (84.1)
  - unsupervised fine-tuning: 78.2 (85.1)

#### summary

- bag-of-words and inverted index is only a crude form of approximate nearest neighbor search
- global descriptors are compact and fast, but do not perform as well as local descriptors
- pooling CNN representations is best at last convolutional layers:
   MAC, R-MAC, SPoC\*, CroW\*
- fine-tuning with constrastive or triplet loss allows transferring to a new domain and learning to rank as opposed to classify
- now that images are represented by a global descriptor or just a few regional descriptors, graph methods are more applicable than ever
- modeling the manifold explicitly allows unsupervised fine-tuning without labels, auxiliary systems (e.g. SIFT pipeline), or other information (e.g. temporal neighborhood in video)

#### summary

- bag-of-words and inverted index is only a crude form of approximate nearest neighbor search
- global descriptors are compact and fast, but do not perform as well as local descriptors
- pooling CNN representations is best at last convolutional layers:
   MAC, R-MAC, SPoC\*, CroW\*
- fine-tuning with constrastive or triplet loss allows transferring to a new domain and learning to rank as opposed to classify
- now that images are represented by a global descriptor or just a few regional descriptors, graph methods are more applicable than ever
- modeling the manifold explicitly allows unsupervised fine-tuning without labels, auxiliary systems (e.g. SIFT pipeline), or other information (e.g. temporal neighborhood in video)

#### summary

- bag-of-words and inverted index is only a crude form of approximate nearest neighbor search
- global descriptors are compact and fast, but do not perform as well as local descriptors
- pooling CNN representations is best at last convolutional layers:
   MAC, R-MAC, SPoC\*, CroW\*
- fine-tuning with constrastive or triplet loss allows transferring to a new domain and learning to rank as opposed to classify
- now that images are represented by a global descriptor or just a few regional descriptors, graph methods are more applicable than ever
- modeling the manifold explicitly allows unsupervised fine-tuning without labels, auxiliary systems (e.g. SIFT pipeline), or other information (e.g. temporal neighborhood in video)