

lecture 10: image retrieval and manifold learning

deep learning for vision

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Inria Rennes-Bretagne Atlantique

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outline

background

pooling

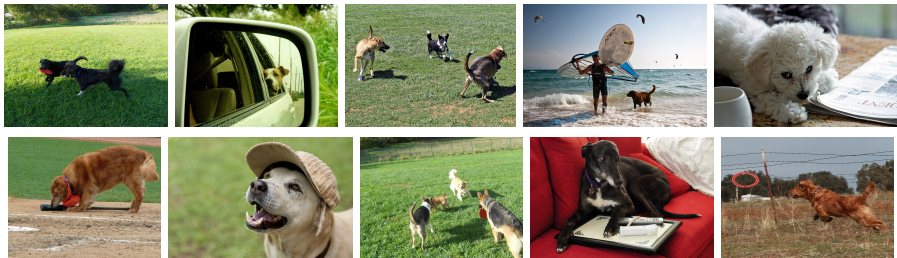
manifold learning

fine-tuning

graph-based methods

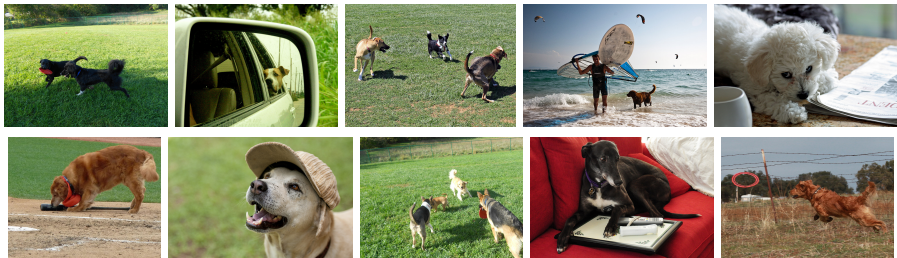
background

image classification challenges



- scale
- viewpoint
- occlusion
- clutter
- lighting
- number of instances
- texture/color
- pose
- deformability
- intra-class variability

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image retrieval challenges



- scale
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- distinctiveness
- distractors

main difference to classification:

- no intra-class variability

image retrieval challenges



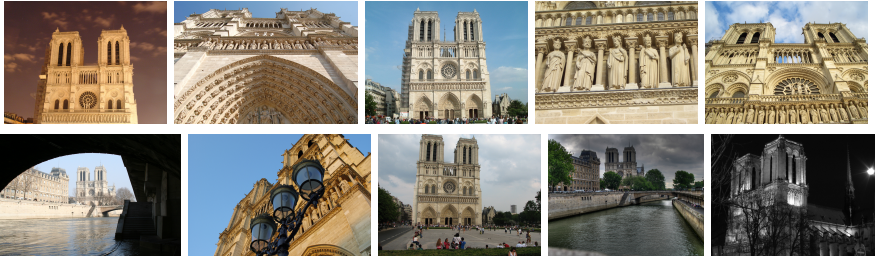
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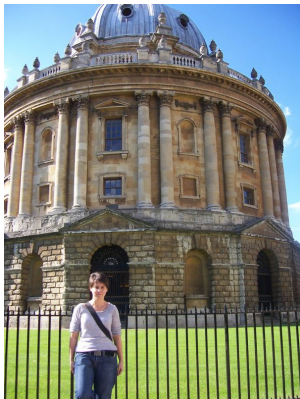
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main difference to classification:

- no intra-class variability

vector quantization \rightarrow visual words



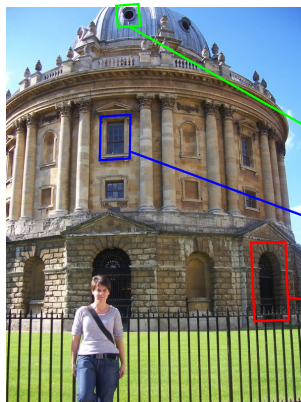
query



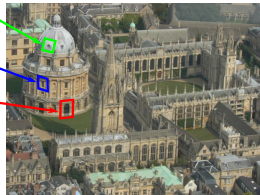
15

- query vs. dataset image

vector quantization \rightarrow visual words



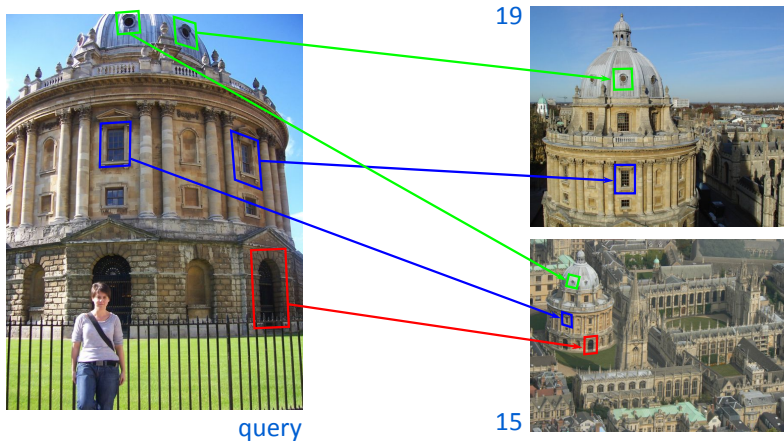
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15

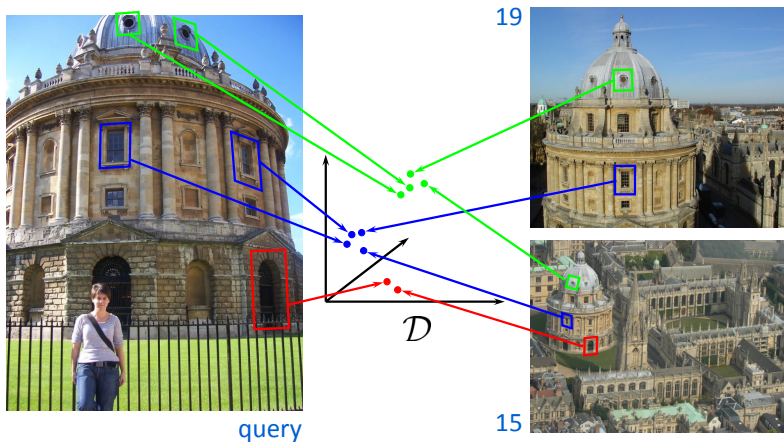
- pairwise descriptor matching

vector quantization \rightarrow visual words



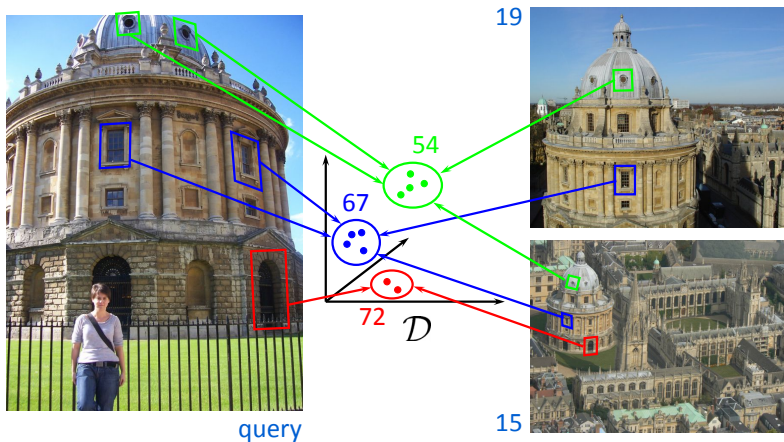
- pairwise descriptor matching for **every** dataset image

vector quantization \rightarrow visual words



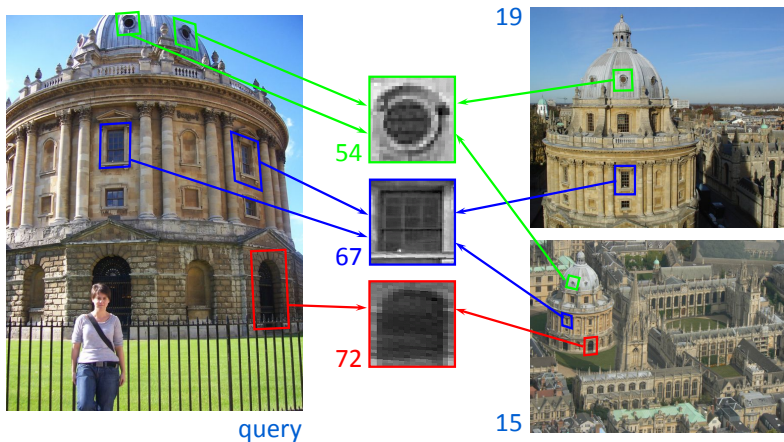
- similar descriptors should all be nearby in the descriptor space

vector quantization \rightarrow visual words



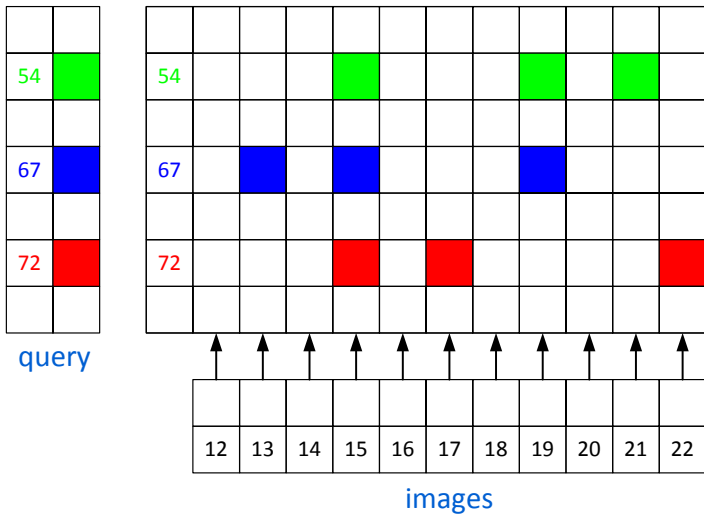
- let's quantize them into visual words

vector quantization \rightarrow visual words

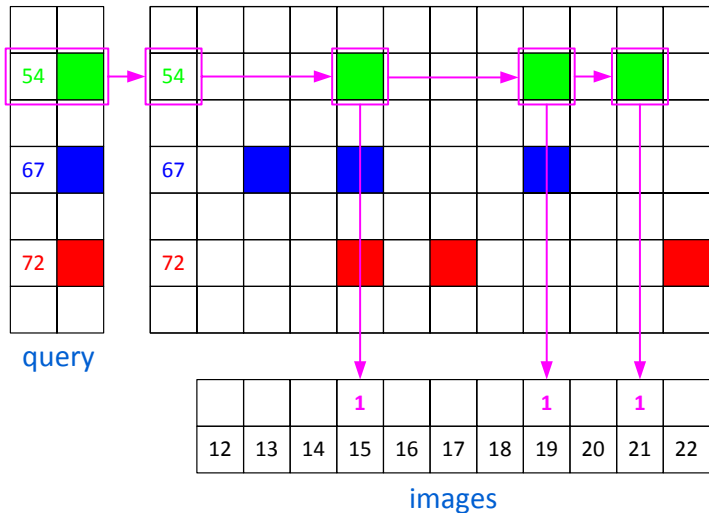


- now visual words act as a proxy; no pairwise matching needed

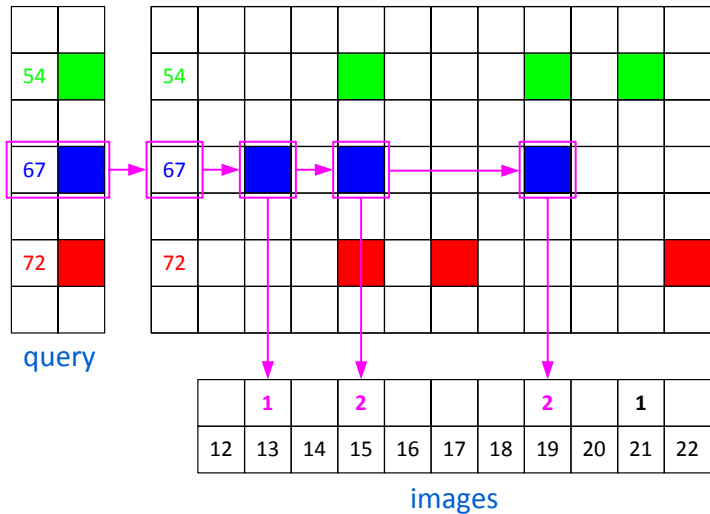
inverted file indexing



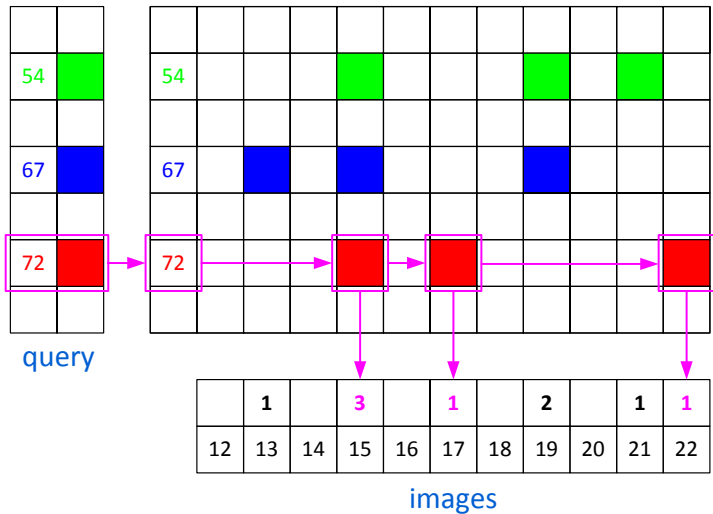
inverted file indexing



inverted file indexing



inverted file indexing



inverted file indexing

54	
67	
72	

54											
67											
72											

query

ranked
shortlist

			1				3													
12	13	14	15	16	17	18	19	20	21	22										

images

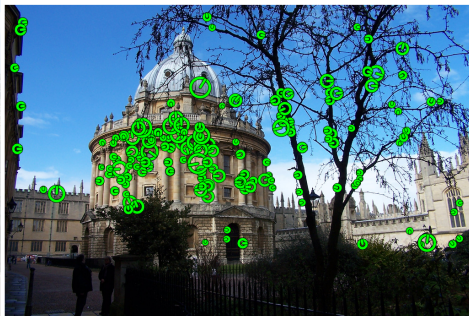
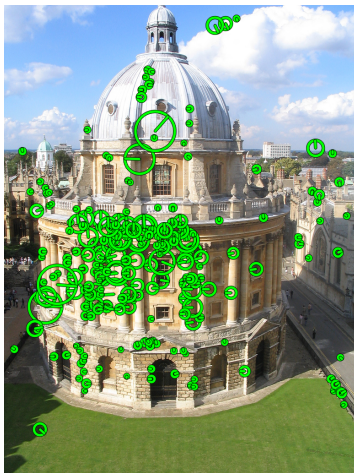
back to geometry: re-ranking



original images

Fischler and Bolles. CACM 1981. Random Sample Consensus: A Paradigm for Model Fitting With Applications to Image Analysis and Automated Cartography.

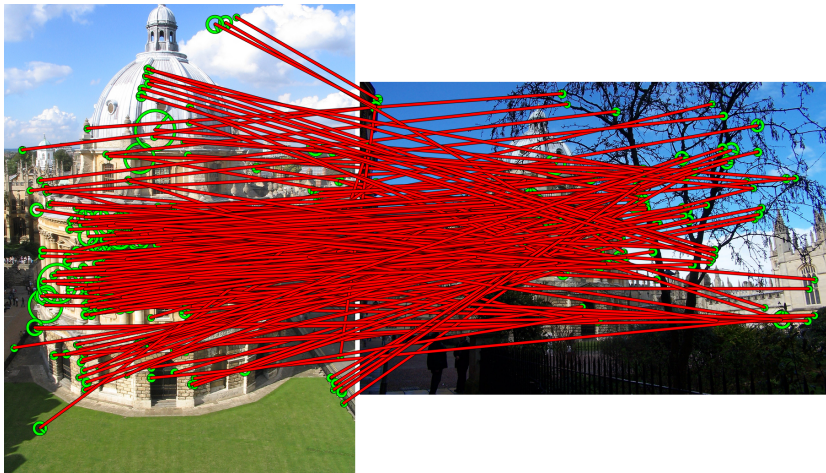
back to geometry: re-ranking



local features

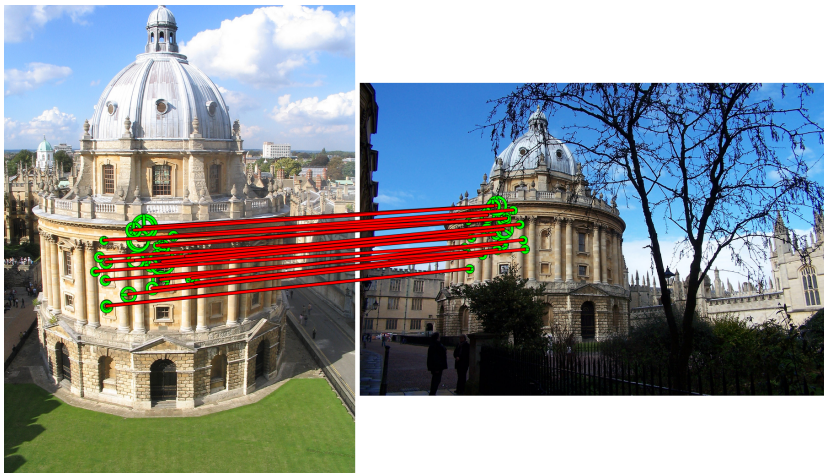
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back to geometry: re-ranking



tentative correspondences: too many

back to geometry: re-ranking



inliers: now more expensive to find

application: location and landmark recognition



Estimated Location Similar Image, Incorrectly geo-tagged Unavailable



Suggested tags: Budon Memorial Fountain, Victoria Tower Gardens, London

Frequent user tags: Victoria Tower Gardens, Budon Memorial Fountain, Winchester Palace, Architecture, Victorian gothic

Similar Images



Similarity: 0.619
Details Original ●●



Similarity: 0.491
Details Original ●●



Similarity: 0.397
Details Original ●●

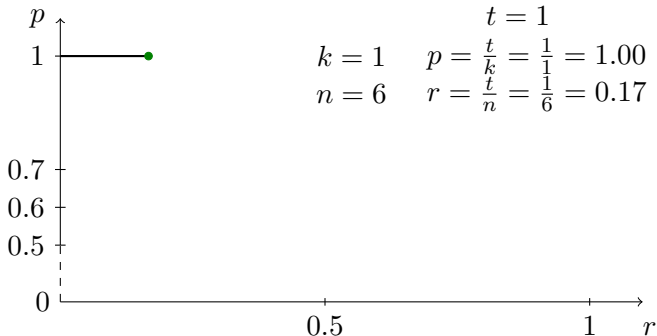


Similarity: 0.385
Details Original ●●

average precision (AP)

- ranked list of items with true/false labels

1	2	3	4	5	6	7	8	9	10	11	12
T	T	F	T	F	F	T	F	T	T	F	F

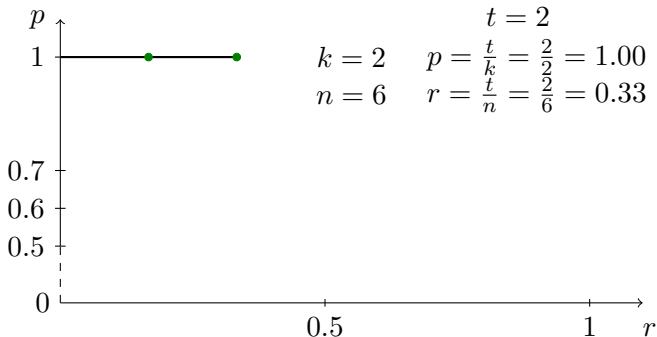


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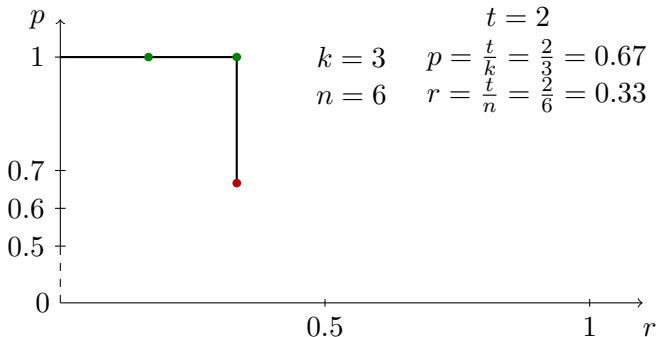


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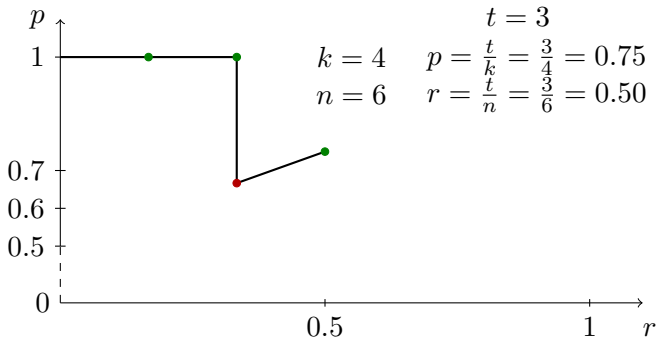


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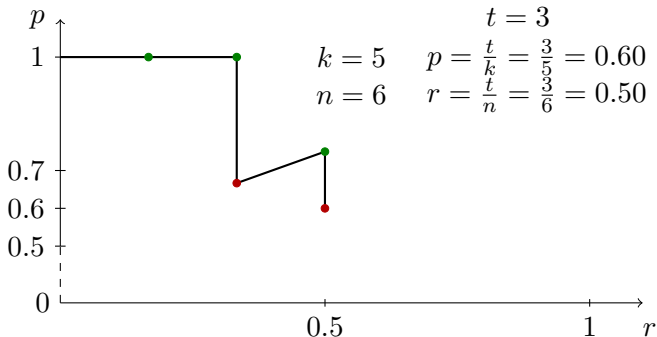


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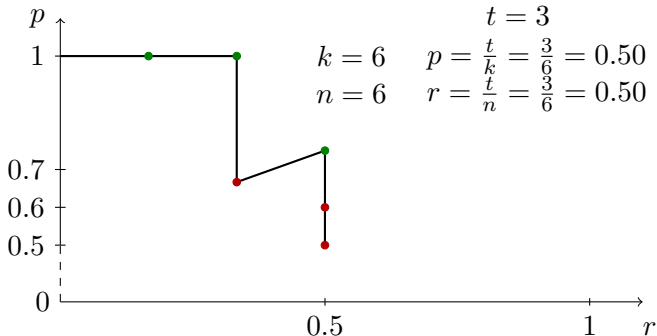


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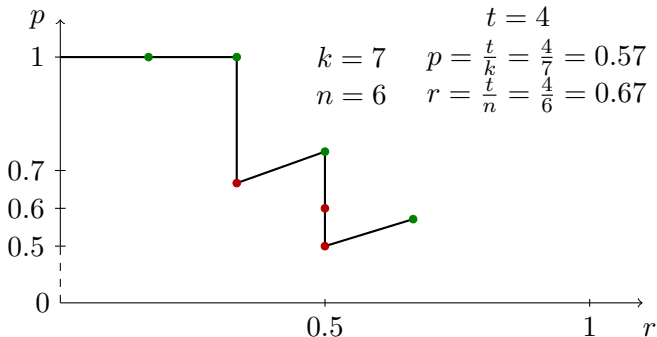


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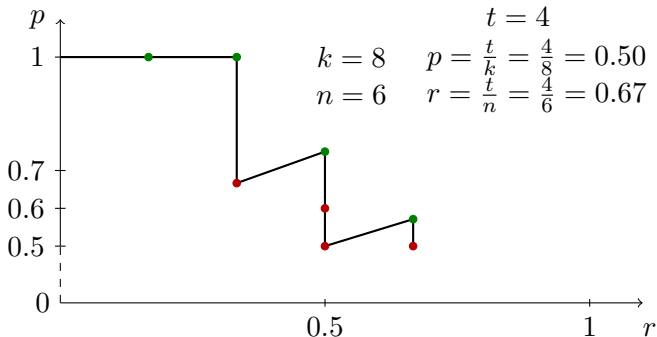


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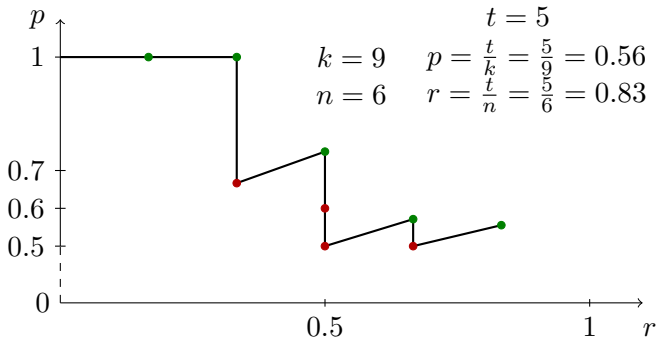


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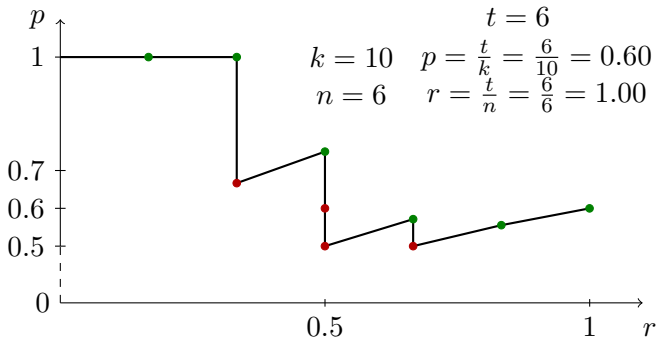


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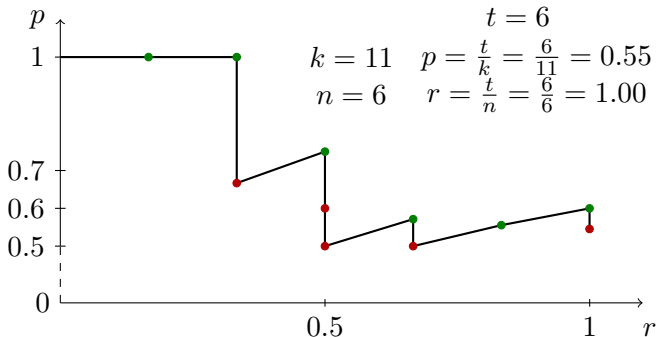


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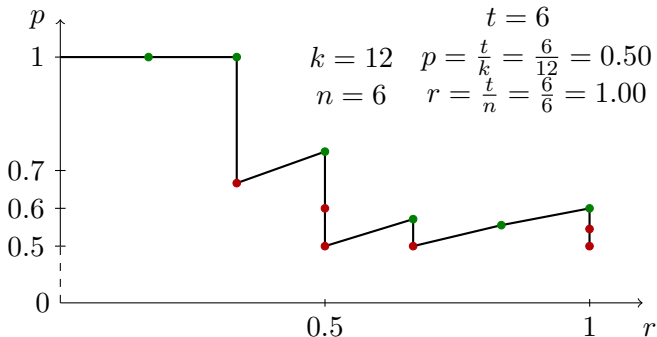


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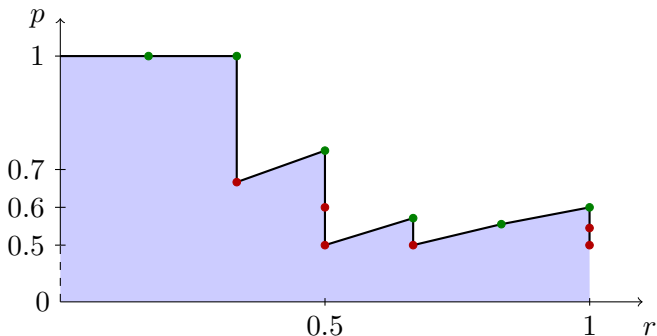


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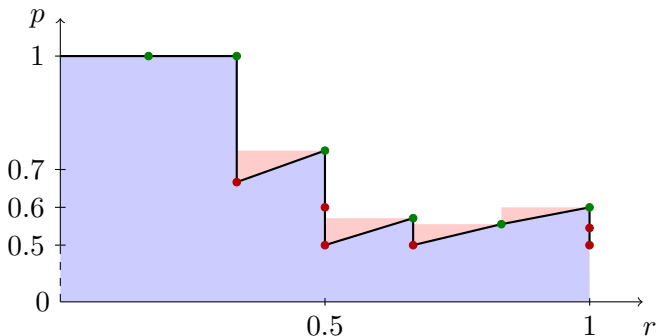


- average precision = area under curve
- the mean average precision (mAP) is the mean over queries

average precision (AP)

- ranked list of items with true/false labels

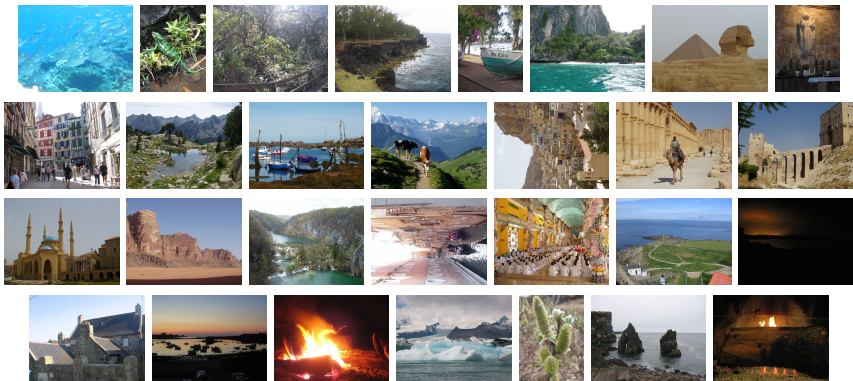
1	2	3	4	5	6	7	8	9	10	11	12
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- average precision = area under curve (filled-in curve)
- the mean average precision (mAP) is the mean over queries

Holidays dataset

[Jégou et al. 2008]



- personal holiday photos, natural and man-made scenes
- 1.5k images, 500 groups, 1 query/group, 1000 positives, 1 ~ 12 positives/query

Oxford buildings dataset

[Philbin et al. 2007]



All Souls



Ashmolean



Balliol



Bodleian



Christ Church



Cornmarket



Hertford



Keble



Magdalen



Pitt Rivers



Radcliffe Camera

- **Oxford5k**: 5k images, 11 landmarks, $5 \times 11 = 55$ queries, 10 ~ 200 positives/query
- **Oxford105k**: 100k additional **distractor** images

Paris dataset

[Philbin et al. 2008]



Defense



Eiffel



Invalides



Louvre



Moulin Rouge



Musée d'Orsay



Notre Dame



Pantheon



Pompidou



Sacré-Cœur



Triomphe

- **Paris6k**: 6k images, 11 landmarks, $5 \times 11 = 55$ queries, 50 ~ 300 positives/query
- **Paris106k**: same 100k **distractor** images as Oxford

Philbin, Chum, Isard, Sivic and Zisserman. CVPR 2008. Lost in Quantization: Improving Particular Object Retrieval in Large Scale Image Databases.

aggregated selective match kernel (ASMK)*

[Tolias et al. 2013]

- residual pooling within cells

$$V(X_c) := \sum_{x \in X_c} r(x) = \sum_{x \in X_c} x - q(x)$$

- nonlinear selectivity between cells

$$K(X, Y) := \gamma(X)\gamma(Y) \sum_{c \in C} w_c \sigma_\alpha \left(\hat{V}(X_c)^\top \hat{V}(Y_c) \right)$$

where $\hat{x} := x/\|x\|$ and σ_α a nonlinear function

triangulation embedding (T-embedding)*

[Jégou and Zisserman 2014]

- normalized residuals, concatenated over cells, pooling over dataset

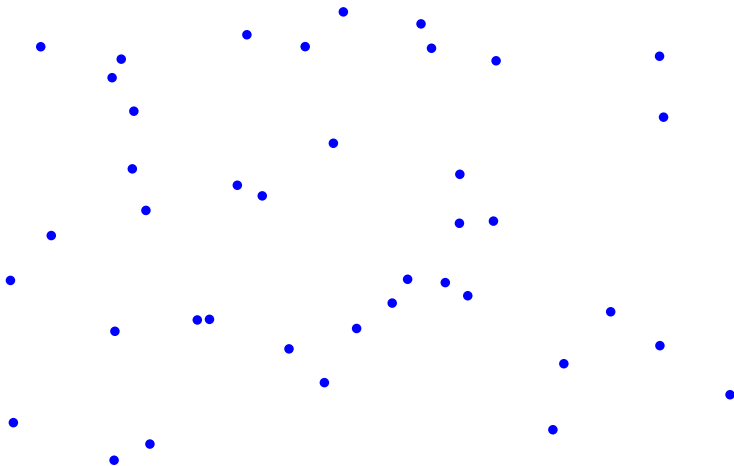
$$R(X) := \sum_{x \in X} (\hat{r}_1(x), \dots, \hat{r}_k(x)) = \sum_{x \in X} \left(\frac{x - c_1}{\|x - c_1\|}, \dots, \frac{x - c_k}{\|x - c_k\|} \right)$$

where $r_j(x) := x - c_j$ and $\hat{x} := x/\|x\|$

- linear kernel, written as inner product

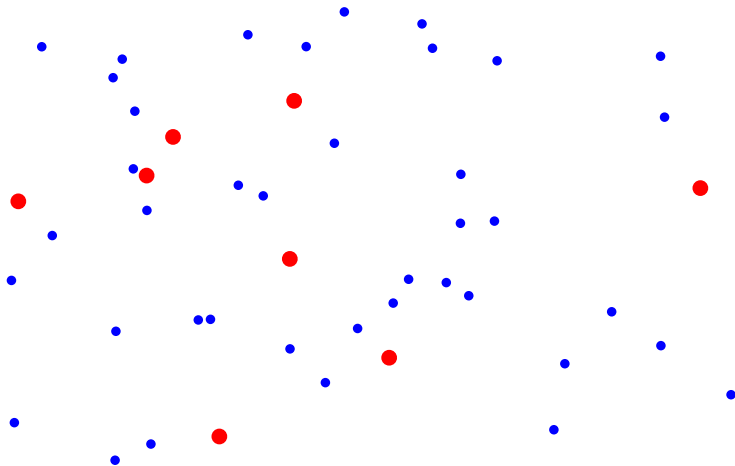
$$K(X, Y) := (\gamma(X)R(X))^T (\gamma(Y)R(Y))$$

triangulation embedding geometry*



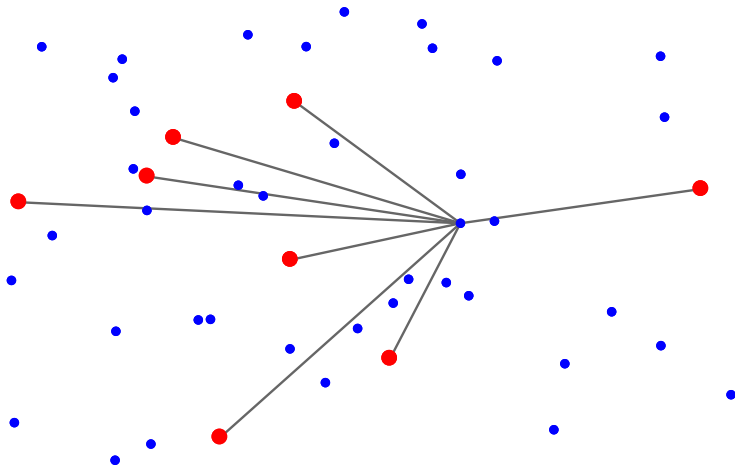
- input vectors – codebook – residuals – normalized residuals

triangulation embedding geometry*



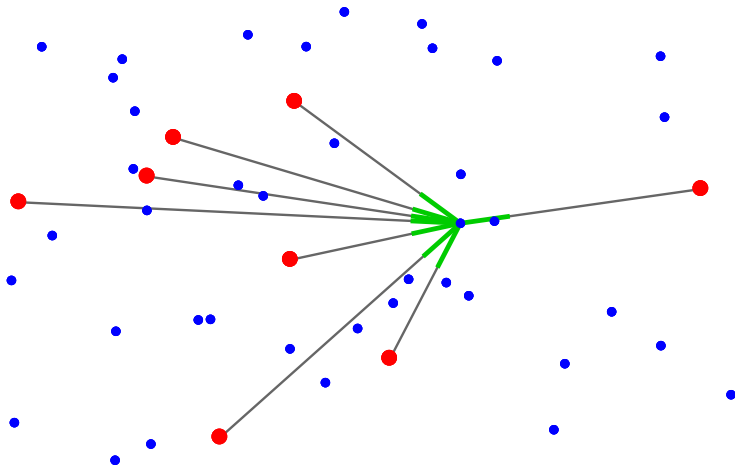
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triangulation embedding geometry*



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triangulation embedding geometry*



- input vectors – codebook – residuals – normalized residuals

performance

- aggregated selective match kernel
 - mAP 81.7 (83.8) mAP on Oxford5k, 78.2 (80.5) on Paris6k, 82.2 (86.5) on Holidays
 - $\sim 2.2\text{k}$ (3.8k) descriptors/image \times 128 dimensions
- triangulation embedding
 - mAP 57.1 (67.6) on Oxford5k, 72.3 (77.1) on Holidays
 - global descriptor, 1920 (8064) dimensions
- no spatial verification or other post-processing

state of the art before deep learning

- bag of words and **inverted index** is only a crude form of approximate nearest neighbor search for each local descriptor, followed by a kernel function
- for good performance, storing **descriptors** is necessary, even compressed
- very good performance achieved with **thousands descriptors**/image
- a **global descriptor**/image allows nearest neighbor search directly on images, but is inferior

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pooling

image ranking by CNN features

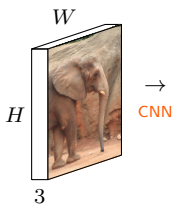
[Krizhevsky et al. 2012]



- 3-channel RGB input, 224×224
- AlexNet pre-trained on ImageNet for classification
- last fully connected layer (fc_6): global descriptor of dimension $k = 4096$

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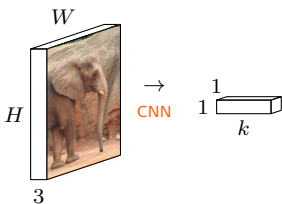
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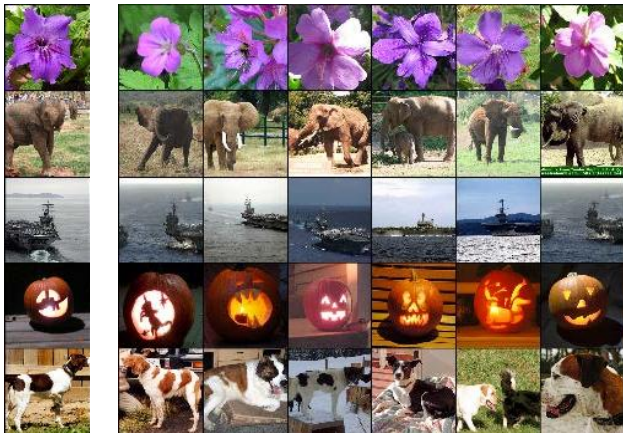
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image ranking by CNN features



- query images
- nearest neighbors in ImageNet according to Euclidean distance

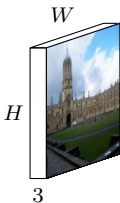
image ranking by CNN features



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neural codes for image retrieval

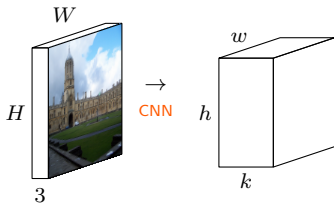
[Babenko et al. 2014]



- 3-channel RGB input, 224×224
- AlexNet last pooling layer, global descriptor of dimension $w \times h \times k = 6 \times 6 \times 256 = 9216$
- alternatively: fully connected layers fc_6, fc_7 , global descriptors of dimension $k' = 4096$ (best is fc_6)
- in each case: PCA-whitening, ℓ_2 normalization

neural codes for image retrieval

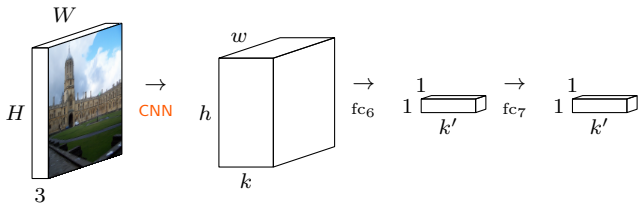
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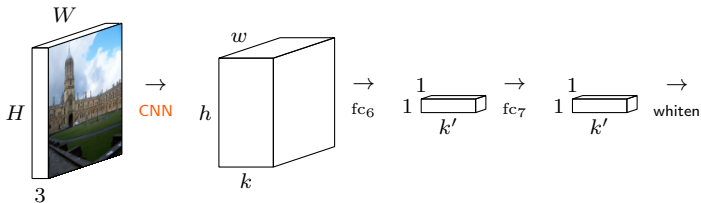
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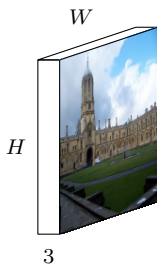
neural codes for image retrieval



- **fine-tuning** by softmax on 672 classes of 200k landmark photos
- outperforms VLAD and Fisher vectors on standard retrieval benchmarks, but still inferior to SIFT local descriptors

regional CNN features

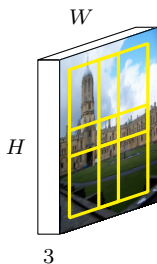
[Razavian et al. 2015]



- 3-channel RGB input, largest square region extracted
- fixed multiscale overlapping regions, warped into $w \times h = 227 \times 227$
- each region yields a $w' \times h' \times k = 36 \times 36 \times 256$ dimensional feature at the last convolutional layer of AlexNet
- global spatial max-pooling
- ℓ_2 -normalization, PCA-whitening of each descriptor

regional CNN features

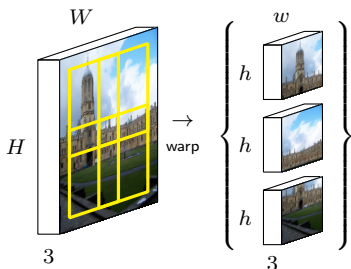
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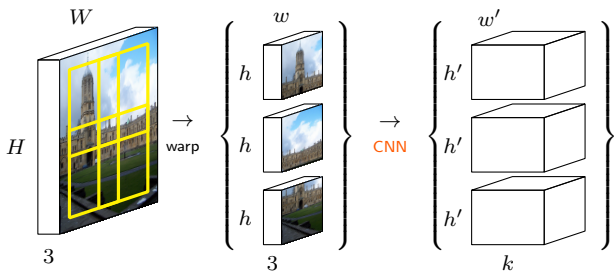
[Razavian et al. 2015]



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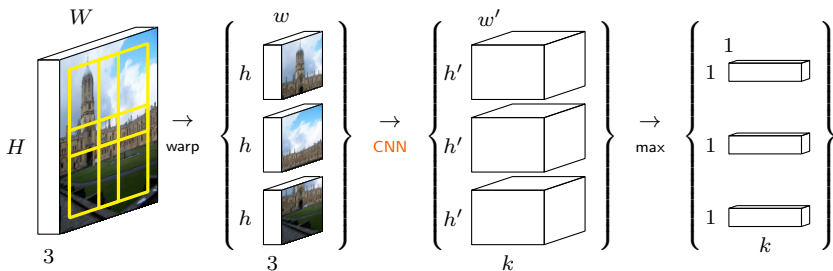
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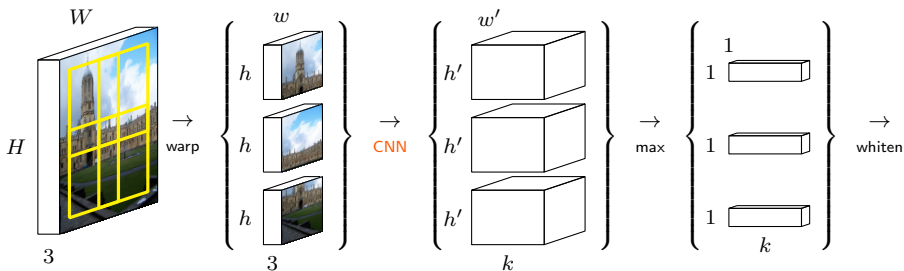
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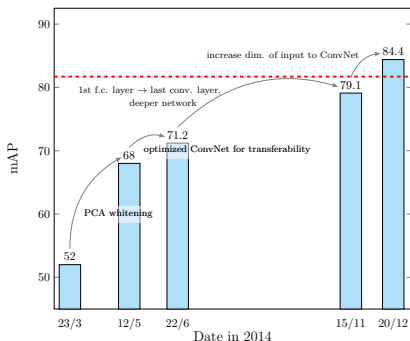
regional CNN features

[Razavian et al. 2015]



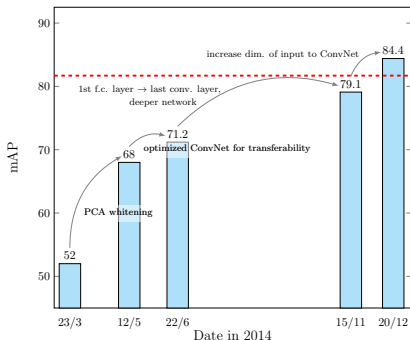
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regional CNN features



- CNN visual representation jumps by more than 30% mAP to outperform standard SIFT pipeline in a few months
- however, this is based on **multiple** regional descriptors per image and **exhaustive** pairwise matching of all descriptors of query and all dataset
- the extraction process is very expensive too

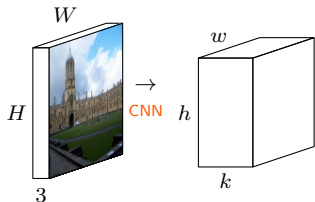
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regional max-pooling (R-MAC)

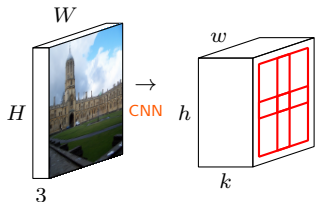
[Tolias et al. 2016]



- VGG-16 last convolutional layer, $k = 512$
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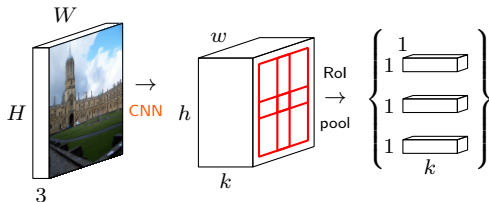
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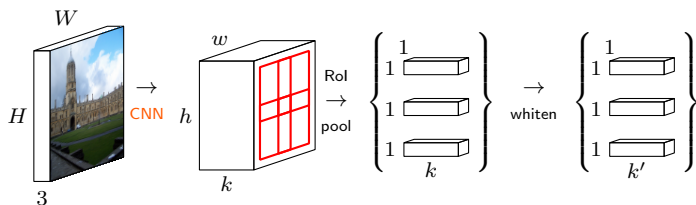
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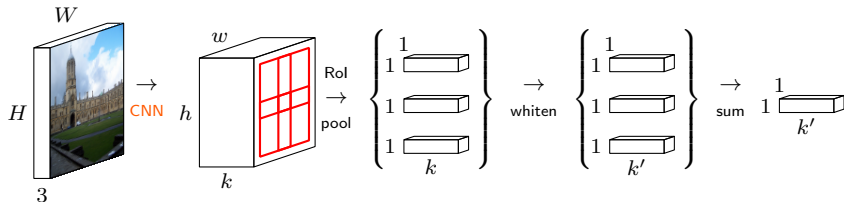
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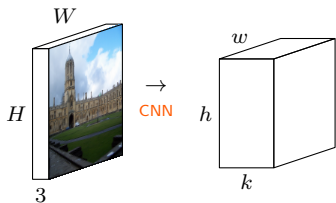
regional max-pooling (R-MAC)

[Tolias et al. 2016]



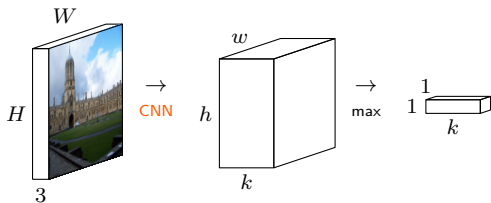
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global max-pooling (MAC)



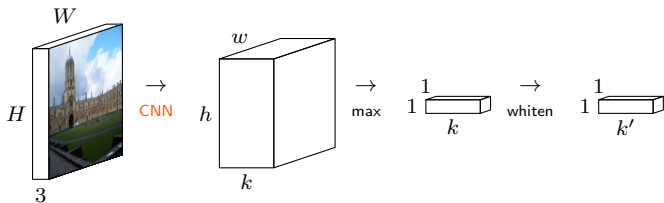
- VGG-16 last convolutional layer, $k = 512$
- global spatial max-pooling
- ℓ_2 -normalization, PCA-whitening, ℓ_2 -normalization
- MAC: maximum activation of convolutions

global max-pooling (MAC)



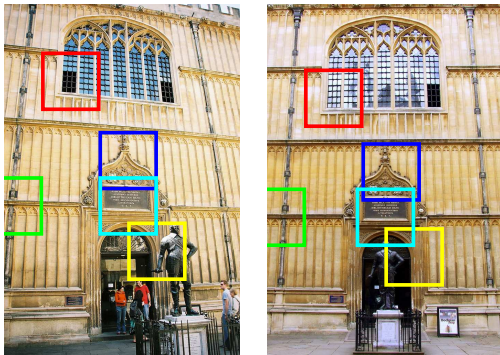
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global max-pooling (MAC)



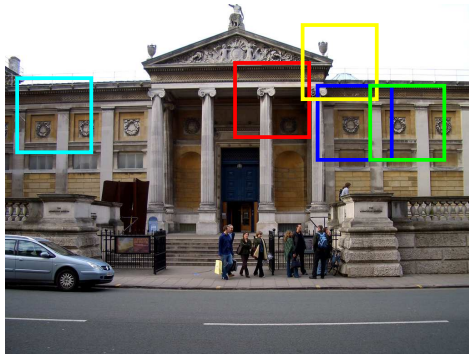
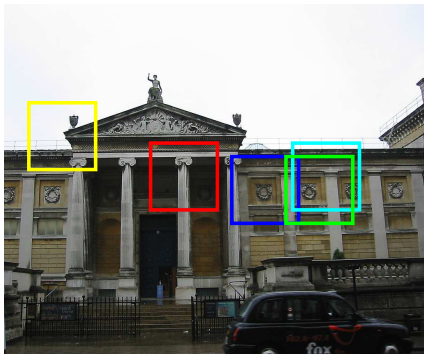
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global max-pooling: matching



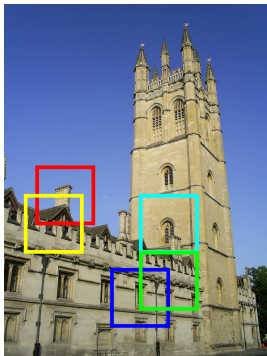
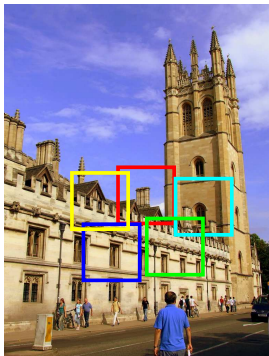
- receptive fields of 5 components of MAC vectors that contribute most to image similarity

global max-pooling: matching



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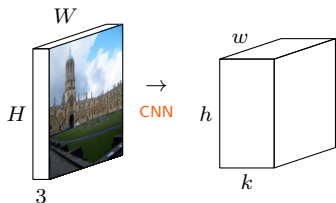
global max-pooling: matching



- receptive fields of 5 components of MAC vectors that contribute most to image similarity

global sum-pooling (SPoC)*

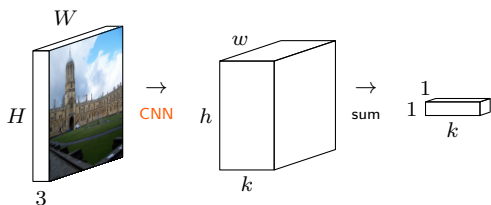
[Babenko and Lempitsky 2015]



- VGG-19 last convolutional layer, $k = 512$
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- SPoC: sum-pooled convolutional features

global sum-pooling (SPoC)*

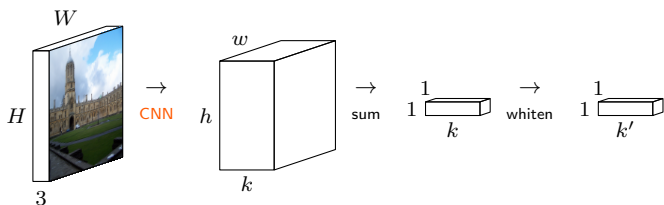
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global sum-pooling (SPoC)*

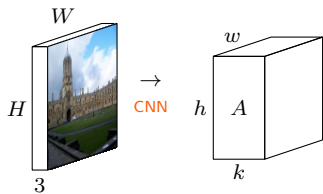
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cross-dimensional weighting (CroW)*

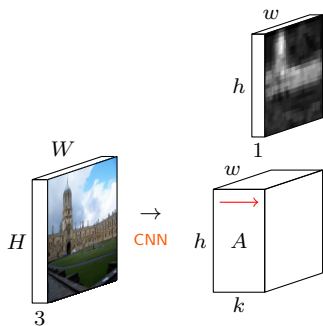
[Kalantidis et al. 2016]



- VGG-16 feature map A , last pooling layer, $k = 512$
- spatial weights F , channel weights w , weighted feature map
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cross-dimensional weighting (CroW)*

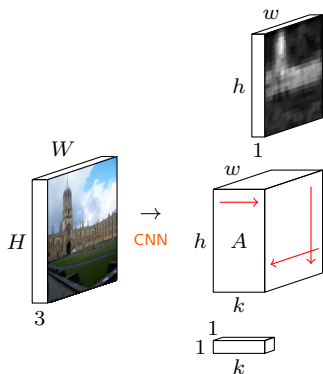
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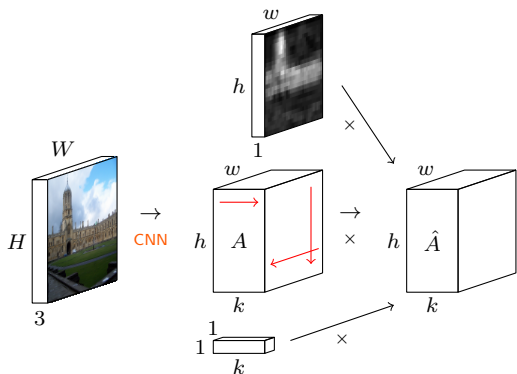
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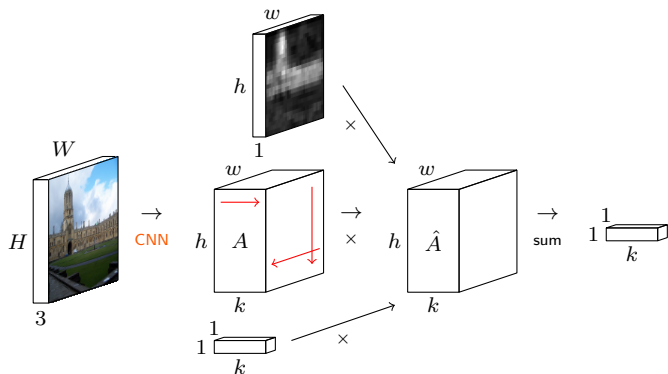
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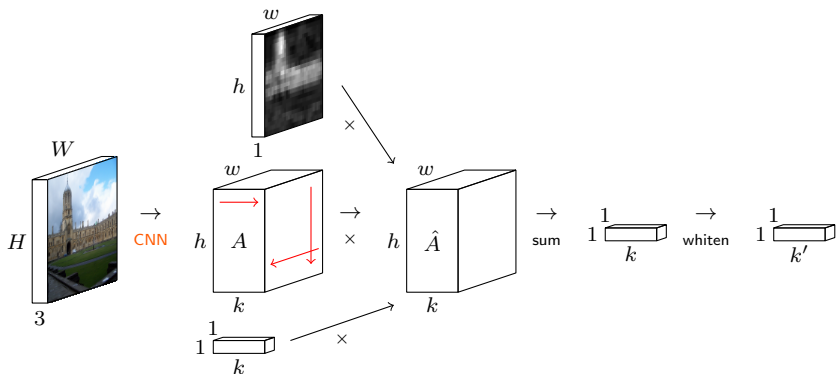
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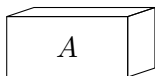
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- spatial weights (visual saliency)

$$F(x, y) = \sum_k A_k(x, y)$$

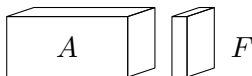
- channel weights (sparsity sensitive)

$$w_j = -\log \left(\epsilon + \sum_{x,y} \mathbb{1}[A_j(x, y)] \right)$$

- weighted feature map

$$\hat{A} = A \times F \times \mathbf{w}$$

cross-dimensional weighting (CroW)*



- **spatial** weights (visual saliency)

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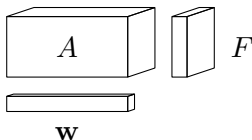
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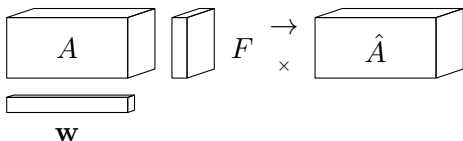
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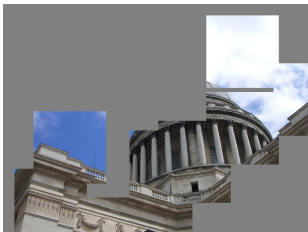
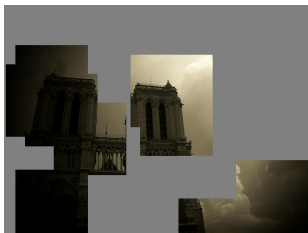
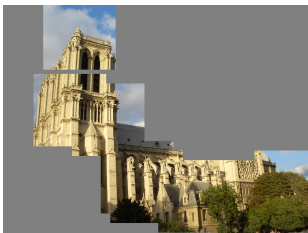
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cross-dimensional weighting (CroW)*



- input image

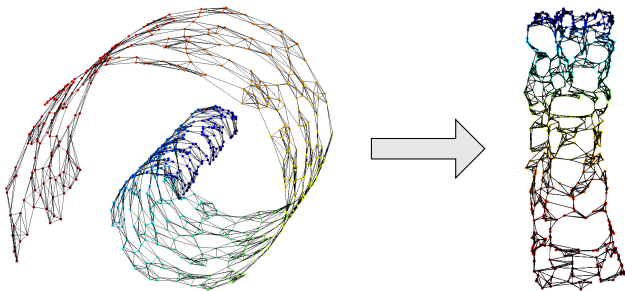
cross-dimensional weighting (CroW)*



- receptive fields of nonzero elements of the 10 channels with the highest sparsity-sensitive weights

manifold learning

manifold learning



- e.g. Isomap: apply PCA to the geodesic (graph) distance matrix
- e.g. kernel PCA: apply PCA to the Gram matrix of a nonlinear kernel
- other **topology-preserving** methods are only focusing on distances to nearest neighbors
- many classic methods use eigenvalue decomposition and most do **not** learn and **explicit mapping** from the input to the embedding space

siamese architecture

[Chopra et al. 2005]

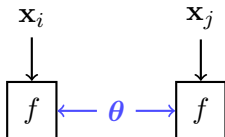
\mathbf{x}_i

\mathbf{x}_j

- an input sample is a pair $(\mathbf{x}_i, \mathbf{x}_j)$
- both $\mathbf{x}_i, \mathbf{x}_j$ go through the same function f with shared parameters θ
- loss ℓ_{ij} is measured on output pair $(\mathbf{y}_i, \mathbf{y}_j)$ and target t_{ij}

siamese architecture

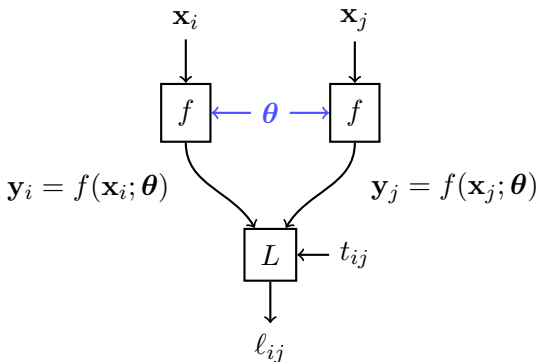
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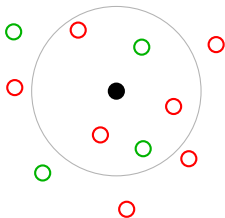
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contrastive loss

[Hadsel et al. 2006]



- input samples \mathbf{x}_i , output vectors $\mathbf{y}_i = f(\mathbf{x}_i; \theta)$
- target variables $t_{ij} = \mathbb{1}[\text{sim}(\mathbf{x}_i, \mathbf{x}_j)]$
- **contrastive loss** is a function of distance $\|\mathbf{y}_i - \mathbf{y}_j\|$ only

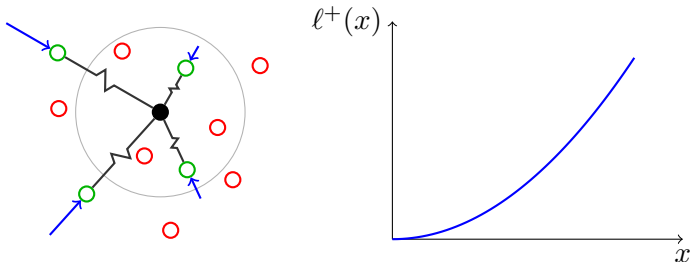
$$\ell_{ij} = L((\mathbf{y}_i, \mathbf{y}_j), t_{ij}) = \ell(\|\mathbf{y}_i - \mathbf{y}_j\|, t_{ij})$$

- **similar** samples are **attracted**

$$\ell(x, t) = t\ell^+(x) + (1 - t)\ell^-(x) = tx^2 + (1 - t)[m - x]_+^2$$

contrastive loss

[Hadsel et al. 2006]



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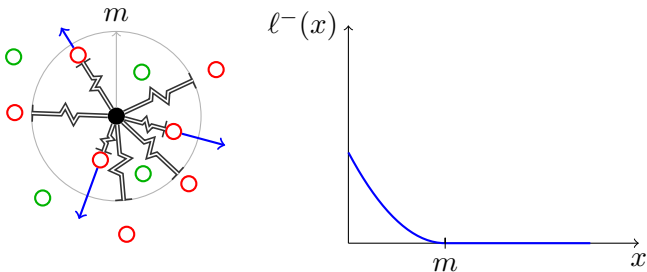
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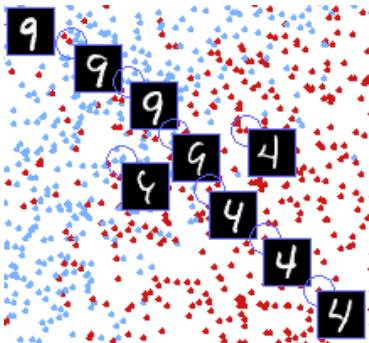
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- **dissimilar** samples are **repelled** if closer than **margin** m

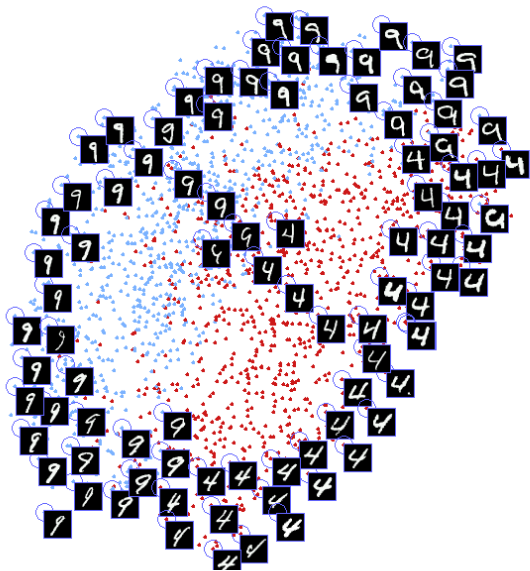
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manifold learning: MNIST

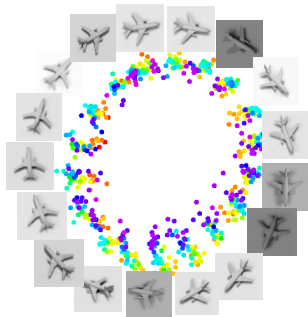


- 3k samples of each of digits 4, 9
- each sample similar to its 5 Euclidean nearest neighbors, and dissimilar to all other points
- 30k similar pairs, 18M dissimilar pairs

manifold learning: MNIST

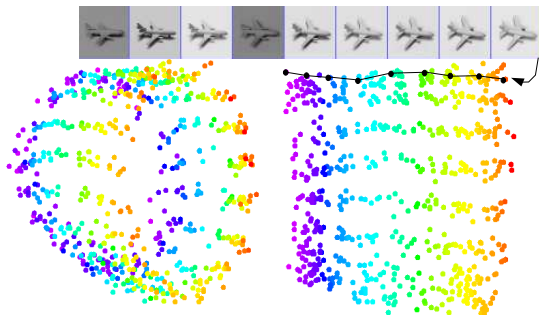


manifold learning: NORB



- 972 images of airplane class: 18 azimuths (every 20°), 9 elevations (in $[30^\circ, 70^\circ]$, every 5°), 6 lighting conditions
- samples similar if taken from contiguous azimuth or elevation, regardless of lighting
- 11k similar pairs, 206M dissimilar pairs
- cylinder in 3d: **azimuth on circumference**, elevation on height

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triplet architecture

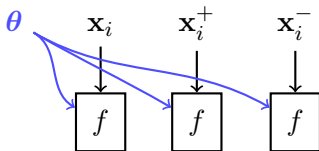
[Wang et al. 2014]

$$\mathbf{x}_i \quad \mathbf{x}_i^+ \quad \mathbf{x}_i^-$$

- an input sample is a **triplet** $(\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-)$
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through the **same** function f with **shared** parameters θ
- loss ℓ_i measured on output triplet $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

triplet architecture

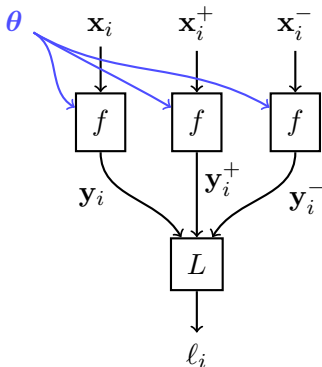
[Wang et al. 2014]



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triplet architecture

[Wang et al. 2014]



- an input sample is a **triplet** (x_i, x_i^+, x_i^-)
- x_i, x_i^+, x_i^- go through the **same** function f with **shared** parameters θ
- loss l_i measured on output triplet (y_i, y_i^+, y_i^-)

triplet loss

- input “anchor” \mathbf{x}_i , output vector $\mathbf{y}_i = f(\mathbf{x}_i; \boldsymbol{\theta})$
- positive $\mathbf{y}_i^+ = f(\mathbf{x}_i^+; \boldsymbol{\theta})$, negative $\mathbf{y}_i^- = f(\mathbf{x}_i^-; \boldsymbol{\theta})$
- triplet loss is a function of distances $\|\mathbf{y}_i - \mathbf{y}_i^+\|$, $\|\mathbf{y}_i - \mathbf{y}_i^-\|$ only

$$\ell_i = L(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-) = \ell(\|\mathbf{y}_i - \mathbf{y}_i^+\|, \|\mathbf{y}_i - \mathbf{y}_i^-\|)$$

$$\ell(x^+, x^-) = [m + (x^+)^2 - (x^-)^2]_+$$

so distance $\|\mathbf{y}_i - \mathbf{y}_i^+\|$ should be less than $\|\mathbf{y}_i - \mathbf{y}_i^-\|$ by margin m

- by taking two pairs $(\mathbf{x}_i, \mathbf{x}_i^+)$ and $(\mathbf{x}_i, \mathbf{x}_i^-)$ at a time with targets 1, 0 respectively, the contrastive loss can be written similarly

$$\ell(x^+, x^-) = (x^+)^2 + [m - x^-]^2_+$$

so distance $\|\mathbf{y}_i - \mathbf{y}_i^+\|$ should small and $\|\mathbf{y}_i - \mathbf{y}_i^-\|$ larger than m

triplet loss

- input “anchor” \mathbf{x}_i , output vector $\mathbf{y}_i = f(\mathbf{x}_i; \theta)$
- positive $\mathbf{y}_i^+ = f(\mathbf{x}_i^+; \theta)$, negative $\mathbf{y}_i^- = f(\mathbf{x}_i^-; \theta)$
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unsupervised learning by context prediction

[Doersch et al. 2015]

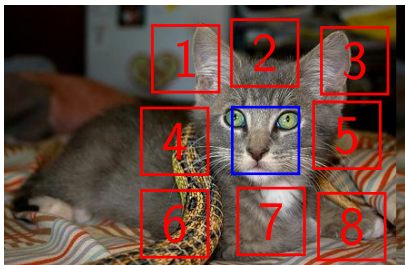


- sample random pairs of patches in one of eight spatial configurations
- patches are randomly jittered and do not overlap
- like **solving a puzzle**, learn to predict the relative position

$$f\left(\begin{array}{c} \\ \\ \end{array}, \begin{array}{c} \\ \\ \end{array}\right) = 3$$

unsupervised learning by context prediction

[Doersch et al. 2015]

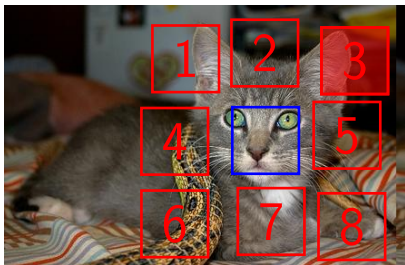


- sample random pairs of patches in one of eight spatial configurations
- patches are randomly jittered and do not overlap
- like solving a puzzle, learn to predict the relative position

$$f\left(\begin{matrix} \\ \\ \end{matrix}, \begin{matrix} \\ \\ \end{matrix}\right) = 3$$

unsupervised learning by context prediction

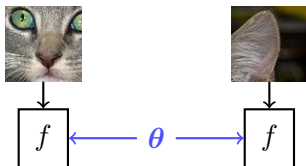
[Doersch et al. 2015]



- sample random pairs of patches in one of eight spatial configurations
- patches are randomly jittered and do not overlap
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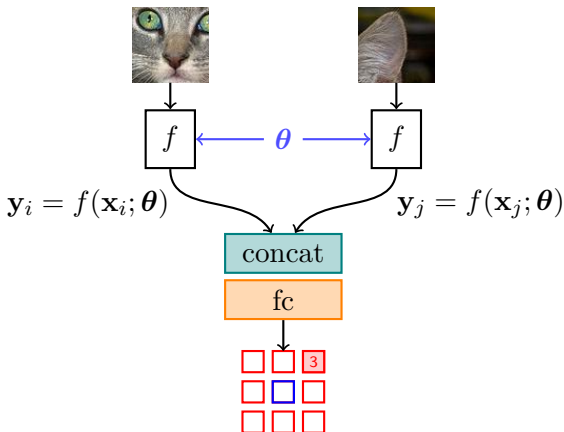
$$f\left(\begin{array}{c} \text{[cat face patch]} \\ \text{[cat ear patch]} \end{array}\right) = 3$$

context prediction: architecture



- network f learned by siamese architecture
- representations are concatenated and followed by softmax classifier, where each spatial configuration is a class

context prediction: architecture



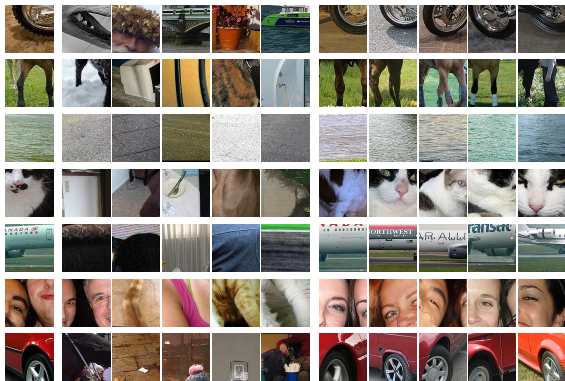
- network f learned by siamese architecture
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context prediction: examples



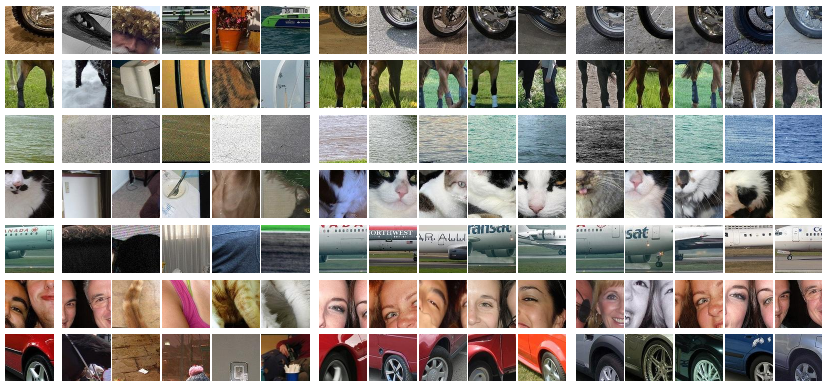
- input image
- nearest neighbors with randomly **initialized** network
- trained by **supervised** classification on ImageNet
- **unsupervised** training from scratch on the context prediction task

context prediction: examples



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- nearest neighbors with randomly **initialized** network
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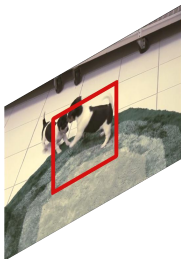
context prediction: examples



- input image
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- **unsupervised** training from scratch on the context prediction task

unsupervised learning on video: tracking

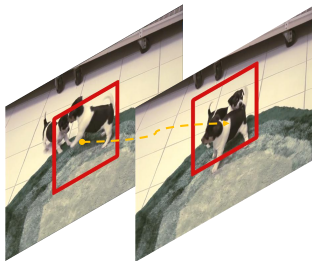
[Wang et al. 2015]



- estimate motion and find the region that contains most motion
- track this region for a number of frames
- generate a pair of matching patches on the first and last frames

unsupervised learning on video: tracking

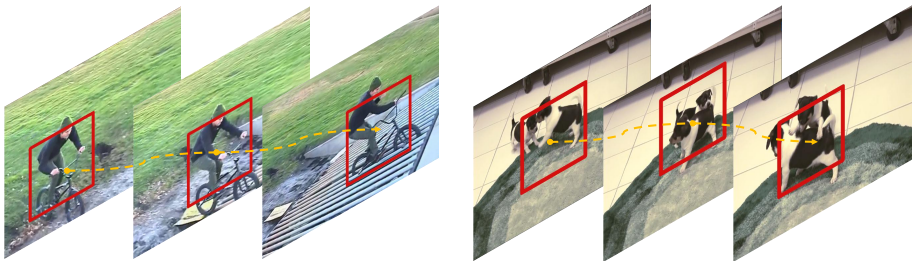
[Wang et al. 2015]



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unsupervised learning on video: tracking

[Wang et al. 2015]



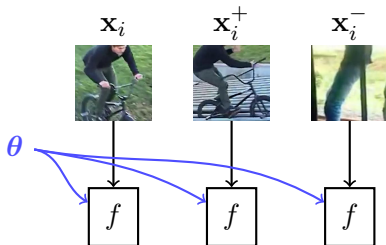
- estimate motion and find the region that contains most motion
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unsupervised learning on video: architecture



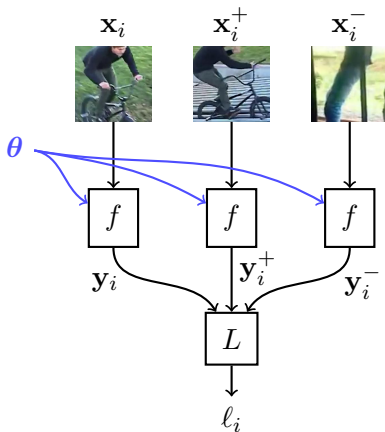
- input query \mathbf{x}_i (first frame), tracked \mathbf{x}_i^+ (last frame), random \mathbf{x}_i^-
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through the same function f with shared parameters θ
- triplet loss ℓ_i measured on output triplet $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

unsupervised learning on video: architecture



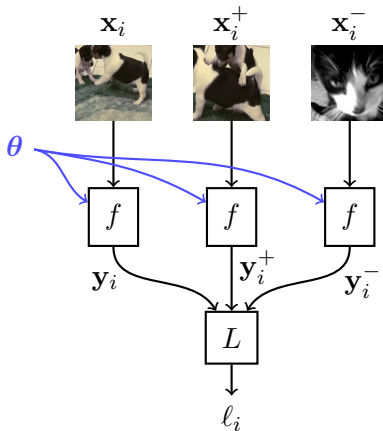
- input query \mathbf{x}_i (first frame), tracked \mathbf{x}_i^+ (last frame), random \mathbf{x}_i^-
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through the **same** function f with **shared** parameters θ
- **triplet loss** ℓ_i measured on output triplet $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

unsupervised learning on video: architecture



- input query x_i (first frame), tracked x_i^+ (last frame), random x_i^-
- x_i, x_i^+, x_i^- go through the **same** function f with **shared** parameters θ
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unsupervised learning on video: architecture



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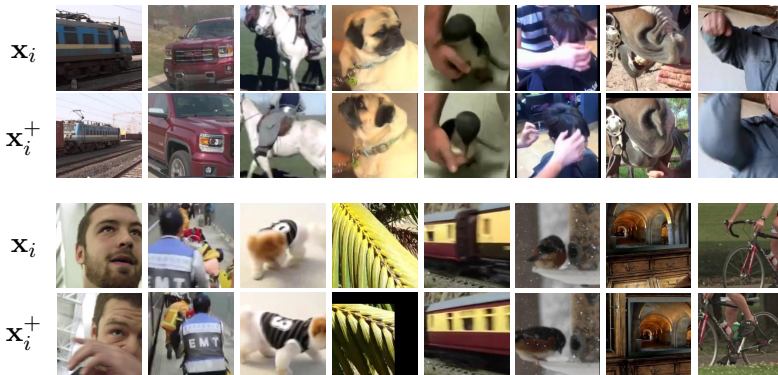
unsupervised learning on video: objective

$$\left\| f\left(\text{img}_1\right) - f\left(\text{img}_2\right) \right\|^2 < \left\| f\left(\text{img}_1\right) - f\left(\text{img}_3\right) \right\|^2 - m$$
$$\left\| f\left(\text{img}_4\right) - f\left(\text{img}_5\right) \right\|^2 < \left\| f\left(\text{img}_4\right) - f\left(\text{img}_6\right) \right\|^2 - m$$

The equations illustrate the objective of unsupervised learning on video. The first equation shows that the squared distance between two frames from the same video (img1 and img2) is less than the squared distance between a frame from the same video (img1) and a frame from a different video (img3), minus a margin m . The second equation shows that the squared distance between two frames from the same video (img4 and img5) is less than the squared distance between a frame from the same video (img4) and a frame from a different video (img6), minus a margin m .

- so, the objective is that squared distance $\|\mathbf{y}_i - \mathbf{y}_i^+\|^2$ is less than $\|\mathbf{y}_i - \mathbf{y}_i^-\|^2$ by margin m

unsupervised learning on video: more examples

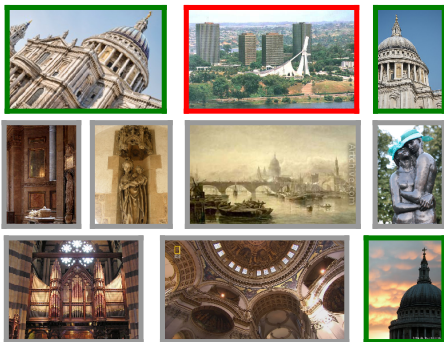


- input query x_i (first frame), tracked x_i^+ (last frame)

fine-tuning

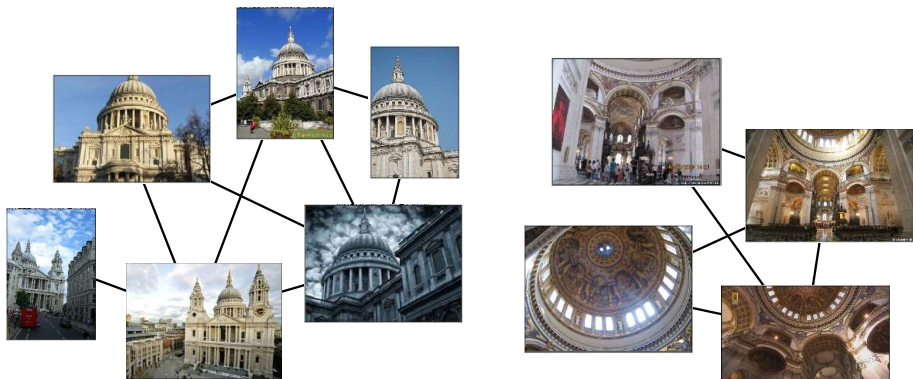
deep image retrieval: dataset cleaning

[Gordo et al. 2016]



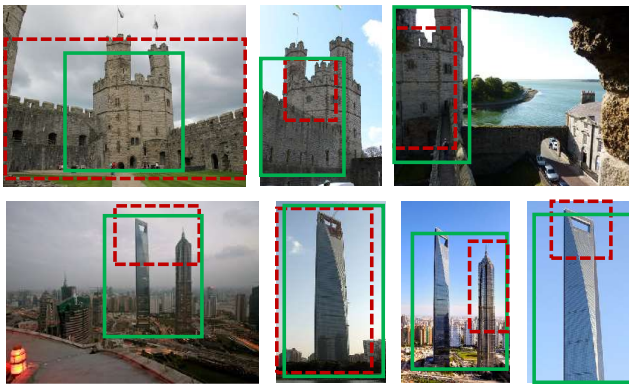
- start from landmark dataset (192k images) and **clean** it (49k images)
- use it to fine-tune a network pre-trained on ImageNet for classification
- **prototypical**, non-prototypical and **incorrect** images per class
- only prototypical are kept to reduce intra-class variability

deep image retrieval: prototypical views



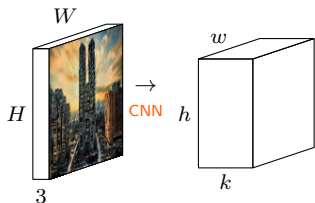
- pairwise match images per class by SIFT descriptors and fast spatial matching
- connect images into a graph and compute the connected components
- keep only the largest component

deep image retrieval: bounding boxes



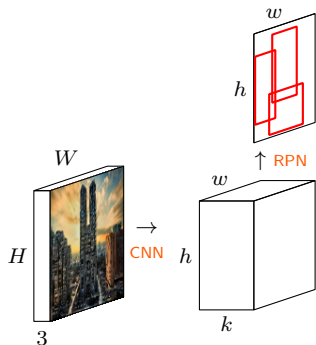
- automatically find object bounding boxes
 - **initialize** with inlier features per image
 - **update** such that boxes are consistent over all matching pairs
- use bounding boxes to train a **region proposal network**

deep image retrieval: network, regions, pooling



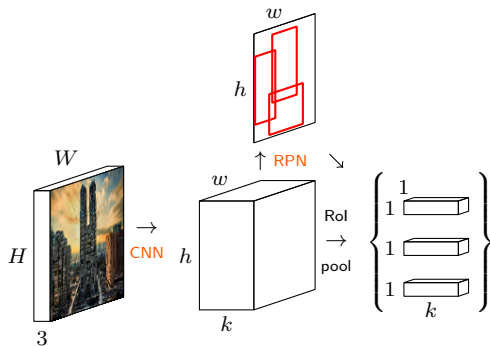
- VGG-16 or ResNet-101 feature maps
- proposals detected on feature maps by RPN and max-pooled
- ℓ_2 -normalization, PCA-whitening (FC layer), ℓ_2 -normalization
- sum-pooling, ℓ_2 -normalization (as in R-MAC)

deep image retrieval: network, regions, pooling



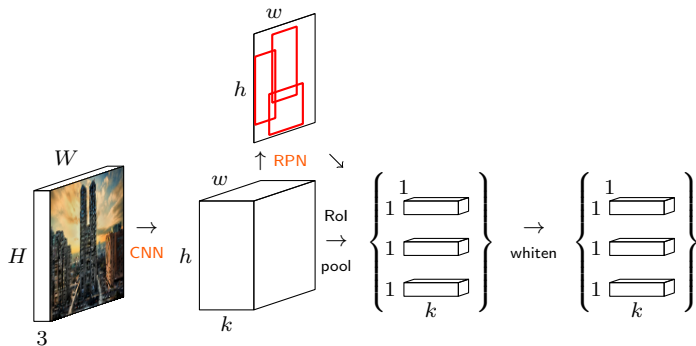
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deep image retrieval: network, regions, pooling



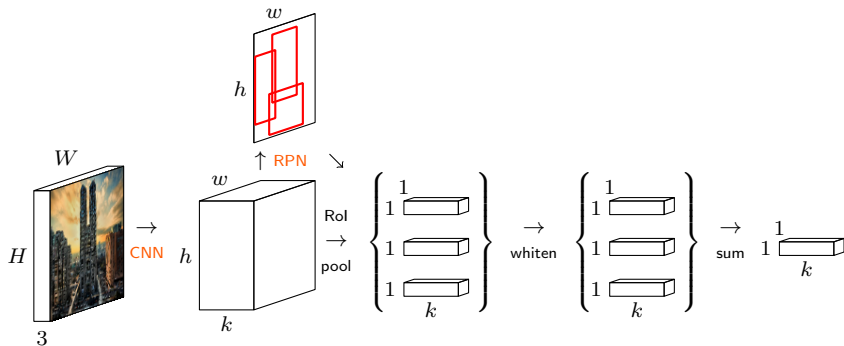
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deep image retrieval: network, regions, pooling



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deep image retrieval: network, regions, pooling



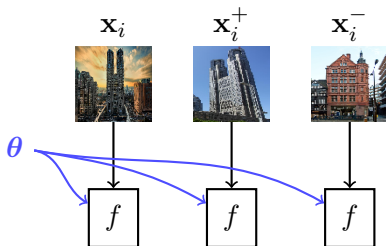
- VGG-16 or ResNet-101 feature maps
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- ℓ_2 -normalization, PCA-whitening (FC layer), ℓ_2 -normalization
- sum-pooling, ℓ_2 -normalization (as in R-MAC)

deep image retrieval: architecture



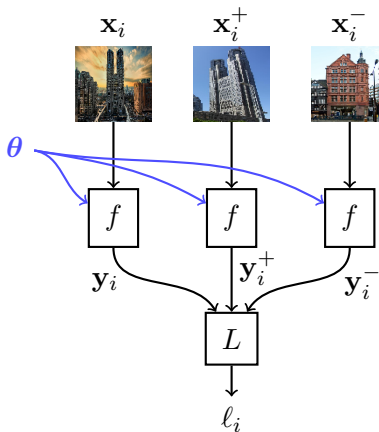
- query \mathbf{x}_i , relevant \mathbf{x}_i^+ (same building), irrelevant \mathbf{x}_i^- (other building)
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through function f including features, RPN, pooling
- triplet loss ℓ_i measured on output $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

deep image retrieval: architecture



- query \mathbf{x}_i , relevant \mathbf{x}_i^+ (same building), irrelevant \mathbf{x}_i^- (other building)
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through function f including features, RPN, pooling
- triplet loss ℓ_i measured on output ($\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-$)

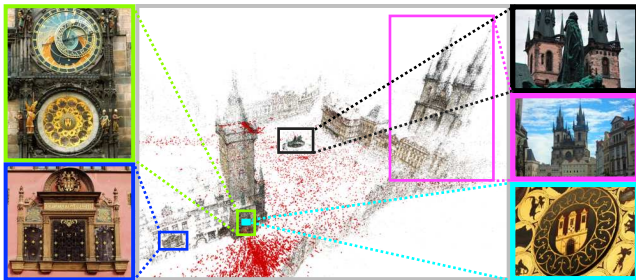
deep image retrieval: architecture



- query \mathbf{x}_i , relevant \mathbf{x}_i^+ (same building), irrelevant \mathbf{x}_i^- (other building)
- $\mathbf{x}_i, \mathbf{x}_i^+, \mathbf{x}_i^-$ go through function f including features, RPN, pooling
- triplet loss ℓ_i measured on output $(\mathbf{y}_i, \mathbf{y}_i^+, \mathbf{y}_i^-)$

learning from bag-of-words: 3d reconstruction

[Radenovic et al. 2016]



- start from an independent dataset of 7.4M images, **no class labels**
- clustering, pairwise matching and **reconstruction** of 713 3d models containing 165k unique images
- **3d models** playing the same role as classes in deep image retrieval
- again, fine-tune a network pre-trained on ImageNet for classification

learning from bag-of-words: positive pairs



- input query
- positive images found in **same model** by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)

learning from bag-of-words: positive pairs



- input query
- positive images found in **same model** by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)

learning from bag-of-words: positive pairs



- input query
- positive images found in **same model** by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)

learning from bag-of-words: positive pairs



- input query
- positive images found in **same model** by minimum MAC distance, maximum inliers, or drawn at random from images having at least a given number of inliers (more challenging)

learning from bag-of-words: negative pairs



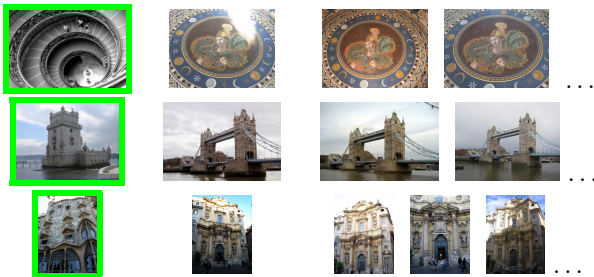
- input query
- negative images found in **different models**
- **hard negatives** are most similar to query, *i.e.* with minimum MAC distance
- hardest negative, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)

learning from bag-of-words: negative pairs



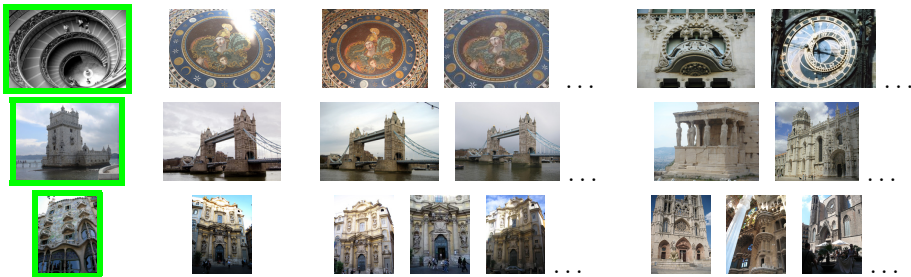
- input query
- negative images found in **different models**
- **hard negatives** are most similar to query, *i.e.* with minimum MAC distance
- **hardest negative**, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)

learning from bag-of-words: negative pairs



- input query
- negative images found in **different models**
- **hard negatives** are most similar to query, *i.e.* with minimum MAC distance
- hardest negative, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)

learning from bag-of-words: negative pairs



- input query
- negative images found in **different models**
- **hard negatives** are most similar to query, *i.e.* with minimum MAC distance
- hardest negative, nearest neighbors from all other models, or nearest neighbors, one per model (higher variability)

learning from bag-of-words: architecture

\mathbf{x}_i

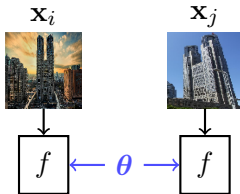


\mathbf{x}_j



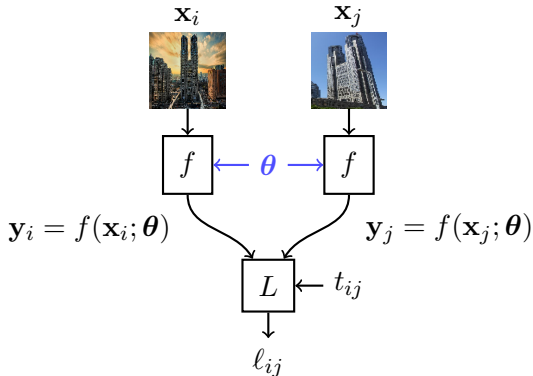
- input $(\mathbf{x}_i, \mathbf{x}_j)$ of relevant or irrelevant images
- both $\mathbf{x}_i, \mathbf{x}_j$ go through function f including features and MAC pooling
- **contrastive loss** ℓ_{ij} measured on output $(\mathbf{y}_i, \mathbf{y}_j)$ and target t_{ij}

learning from bag-of-words: architecture



- input (x_i, x_j) of relevant or irrelevant images
- both x_i, x_j go through function f including features and MAC pooling
- **contrastive loss** l_{ij} measured on output (y_i, y_j) and target t_{ij}

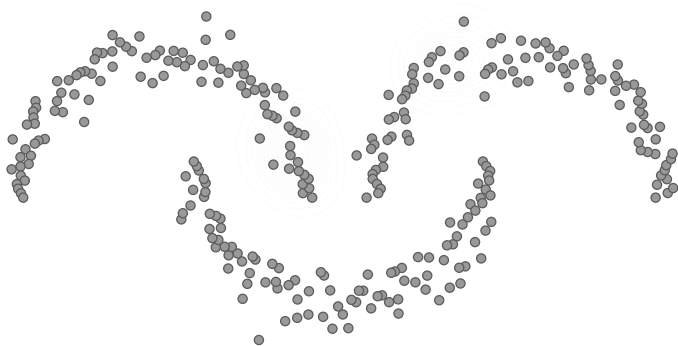
learning from bag-of-words: architecture



- input (x_i, x_j) of relevant or irrelevant images
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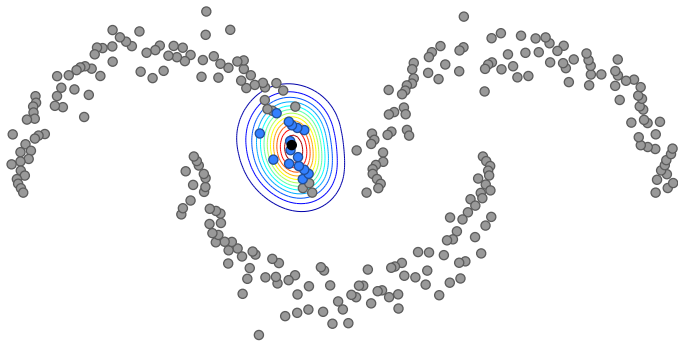
graph-based methods

ranking on manifolds: single query



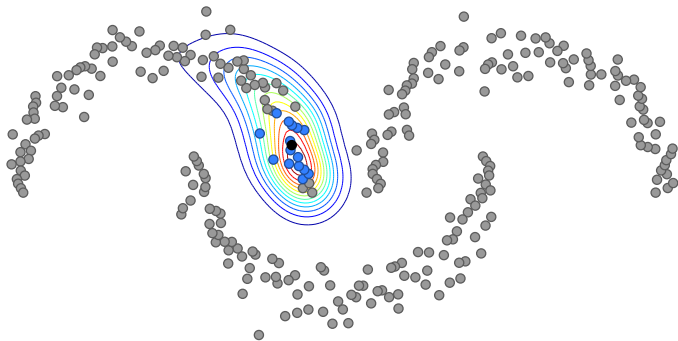
- data points (•), query point (•), nearest neighbors (•)
- iteration $\times 30$

ranking on manifolds: single query



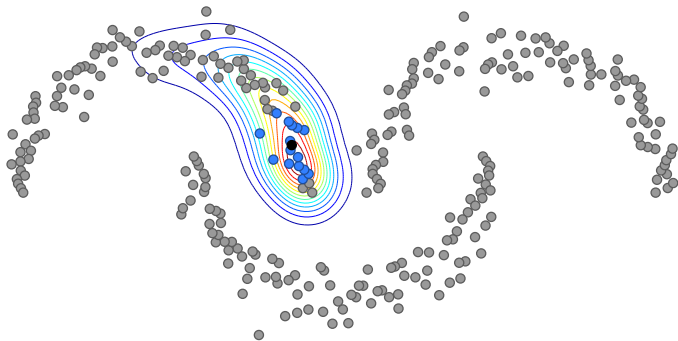
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 0×30

ranking on manifolds: single query



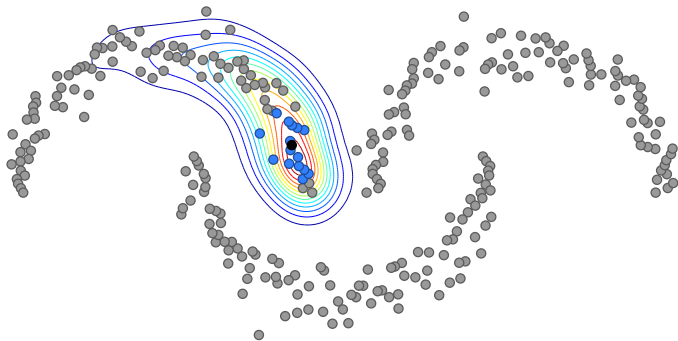
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 1×30

ranking on manifolds: single query



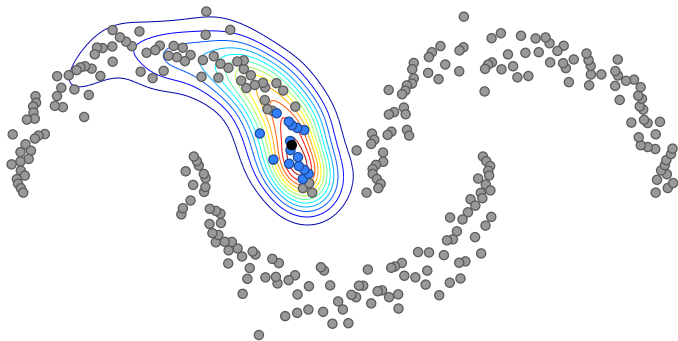
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 2×30

ranking on manifolds: single query



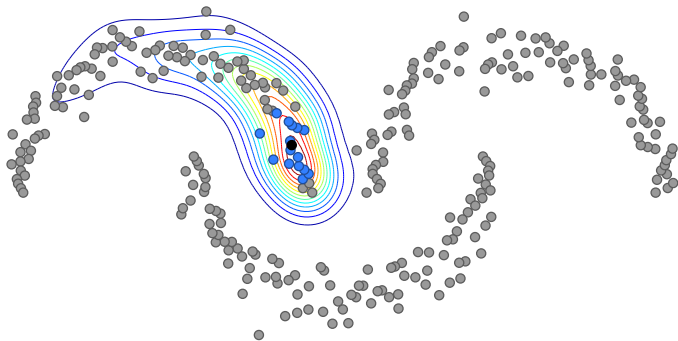
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 3×30

ranking on manifolds: single query



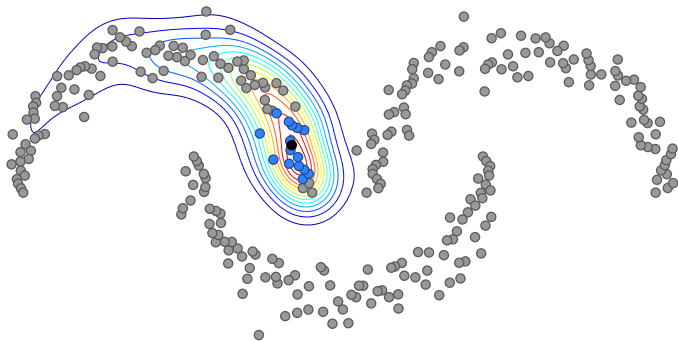
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 4×30

ranking on manifolds: single query



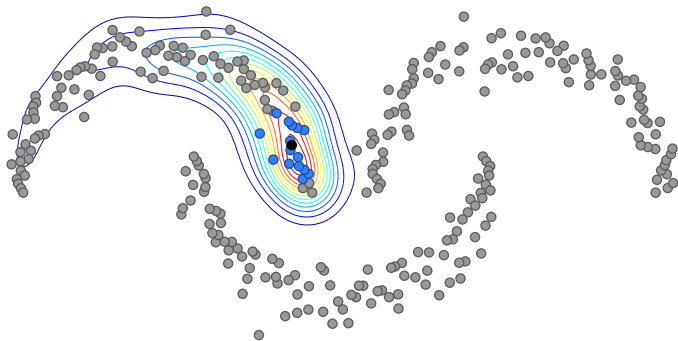
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 5×30

ranking on manifolds: single query



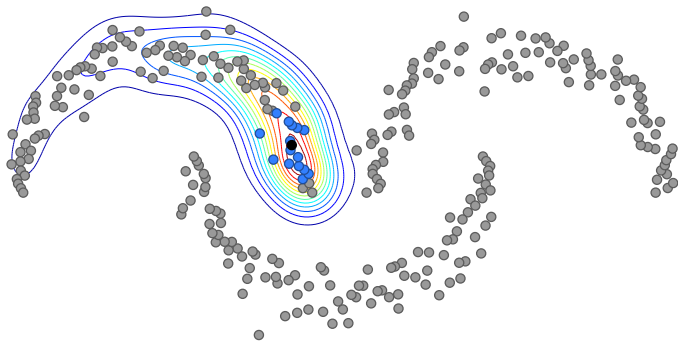
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 6×30

ranking on manifolds: single query



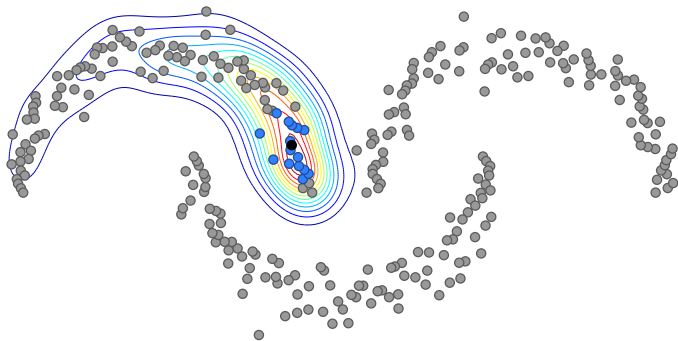
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 7×30

ranking on manifolds: single query



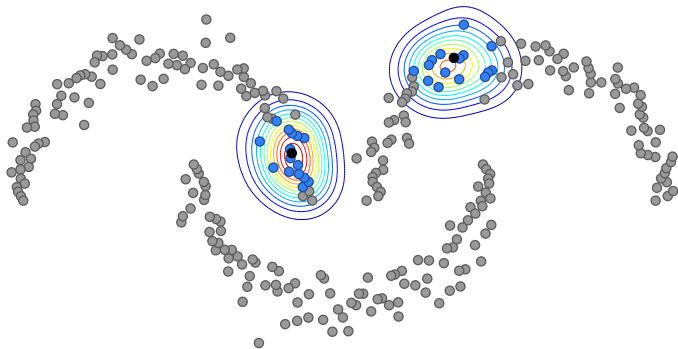
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
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ranking on manifolds: single query



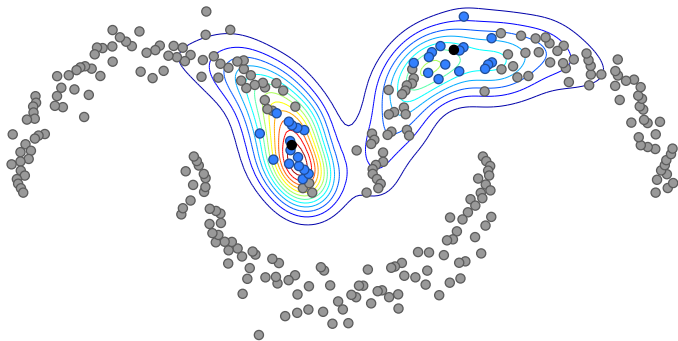
- data points (\bullet), query point (\bullet), nearest neighbors (\bullet)
- iteration 9×30

ranking on manifolds: multiple queries



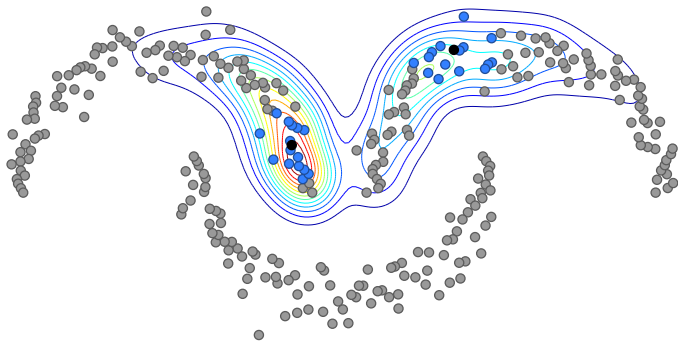
- data points (\bullet), query points (\bullet), nearest neighbors (\bullet)
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ranking on manifolds: multiple queries



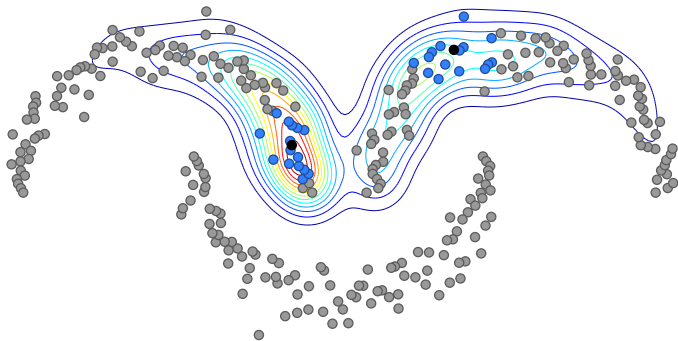
- data points (\bullet), query points (\bullet), nearest neighbors (\bullet)
- iteration 1×30

ranking on manifolds: multiple queries



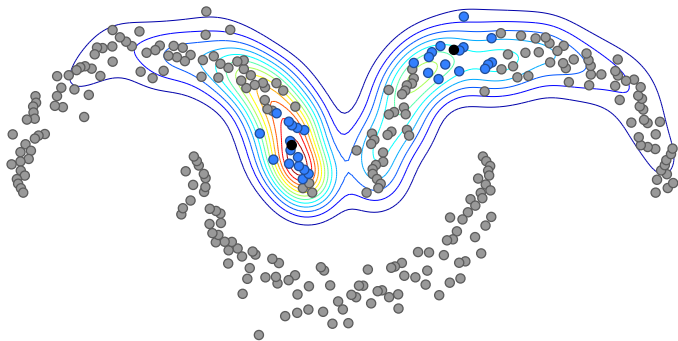
- data points (\circ), query points (\bullet), nearest neighbors (\bullet)
- iteration 2×30

ranking on manifolds: multiple queries



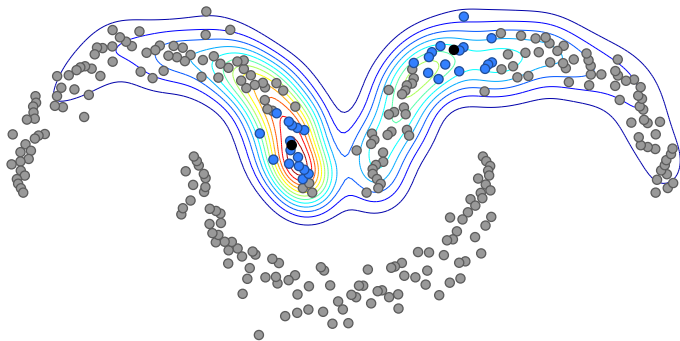
- data points (\bullet), query points (\bullet), nearest neighbors (\bullet)
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ranking on manifolds: multiple queries



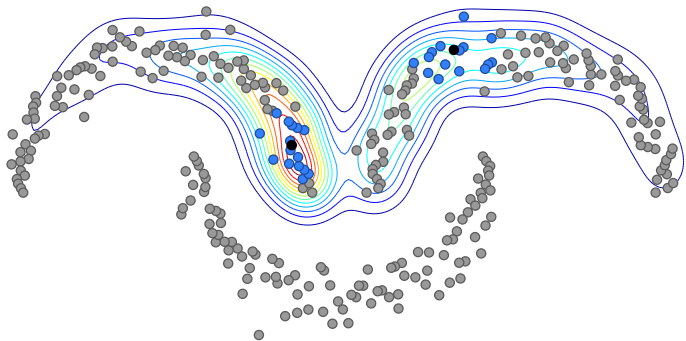
- data points (\bullet), query points (\bullet), nearest neighbors (\bullet)
- iteration 4×30

ranking on manifolds: multiple queries



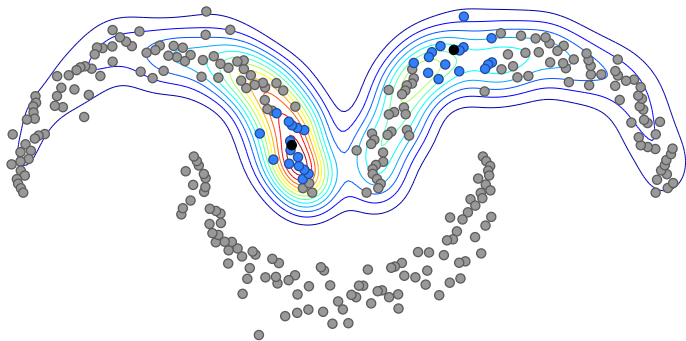
- data points (\bullet), query points (\bullet), nearest neighbors (\bullet)
- iteration 5×30

ranking on manifolds: multiple queries



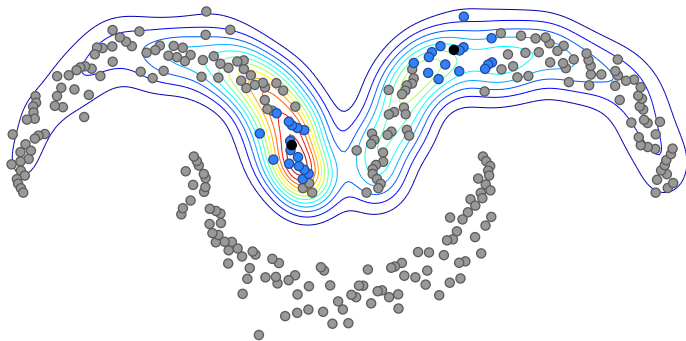
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ranking on manifolds: multiple queries



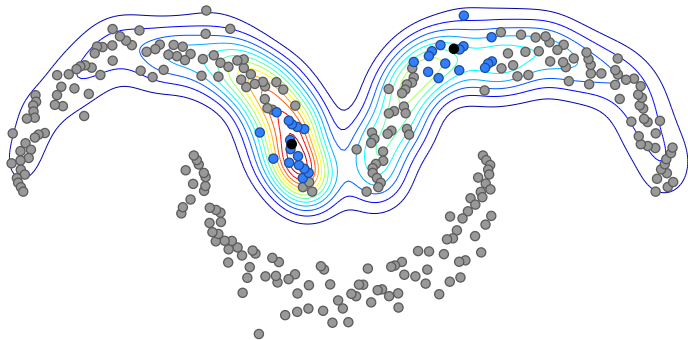
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ranking on manifolds: multiple queries



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ranking on manifolds: multiple queries



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ranking on manifolds: random walk

[Zhou et al. 2003]

- reciprocal nearest neighbor graph on n data points
- non-negative, symmetric, sparse adjacency matrix $W \in \mathbb{R}^{n \times n}$, with zero diagonal (no self-loops)
- symmetrically normalized adjacency matrix

$$\mathcal{W} := D^{-1/2} W D^{-1/2}$$

where $D = \text{diag}(W\mathbf{1})$ is the degree matrix

- query: vector $\mathbf{y} \in \mathbb{R}^n$ with $y_i = \mathbb{1}[i \text{ is query}]$
- random walk: starting with any $\mathbf{f}^{(0)} \in \mathbb{R}^n$, iterate

$$\mathbf{f}^{(\tau)} = \alpha \mathcal{W} \mathbf{f}^{(\tau-1)} + (1 - \alpha) \mathbf{y}$$

where $\alpha \in [0, 1)$ (typically close to 1)

- rank data points by descending order of \mathbf{f}

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ranking as solving a linear system

[Iscen et al. 2017]

- **query**: sparse vector $\mathbf{y} \in \mathbb{R}^n$ with nearest neighbor similarities

$$y_i = \sum_{\mathbf{q} \in Q} s(\mathbf{q}, \mathbf{x}_i) \times \mathbb{1}[\mathbf{x}_i \in \text{NN}_X^k(\mathbf{q})]$$

where $Q, X \subset \mathbb{R}^d$ query/data points, $\mathbf{x}_i \in X$, s similarity function

- regularized **Laplacian**

$$\mathcal{L}_\alpha = \frac{I - \alpha \mathcal{W}}{1 - \alpha}$$

- solve **linear system**

$$\mathcal{L}_\alpha \mathbf{f} = \mathbf{y}$$

by conjugate gradient method

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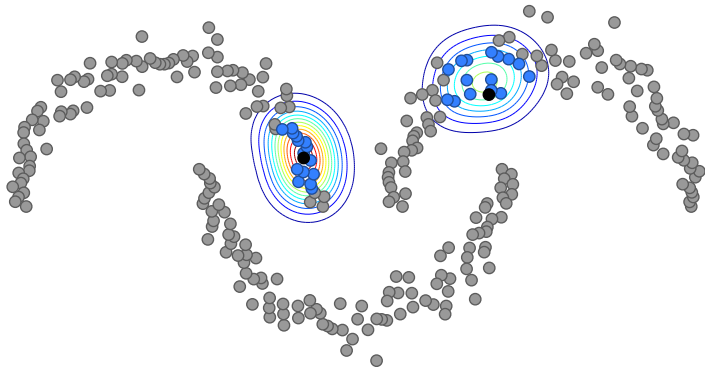
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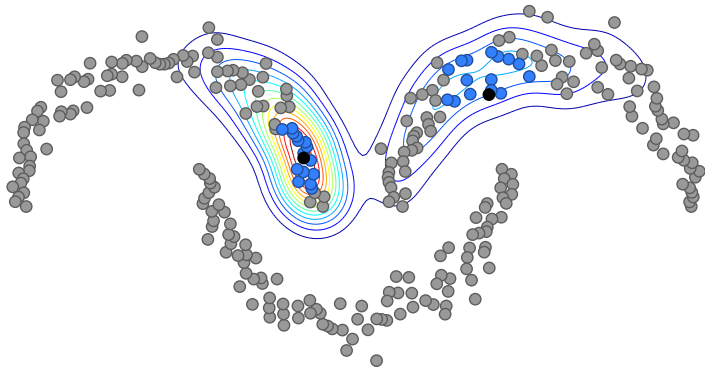
by conjugate gradient method

ranking by conjugate gradient



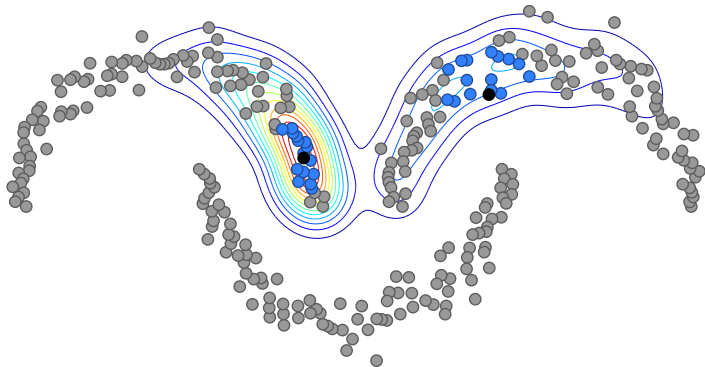
- data points (•), query points (•), nearest neighbors (•)
- iteration 0×2

ranking by conjugate gradient



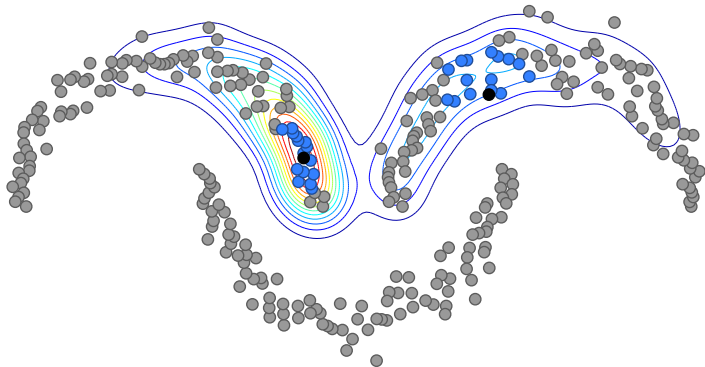
- data points (•), query points (•), nearest neighbors (•)
- iteration 3×2

ranking by conjugate gradient



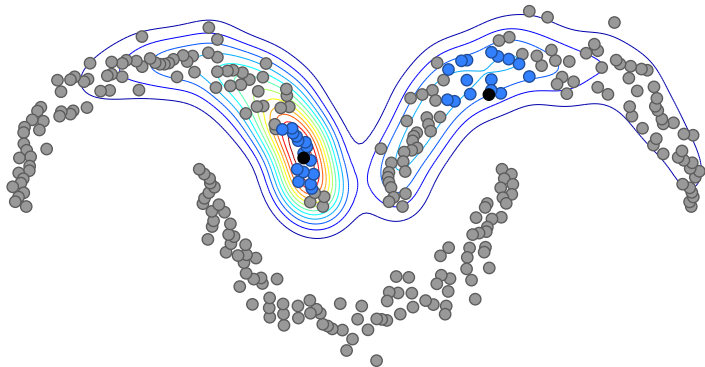
- data points (•), query points (•), nearest neighbors (•)
- iteration 4×2

ranking by conjugate gradient



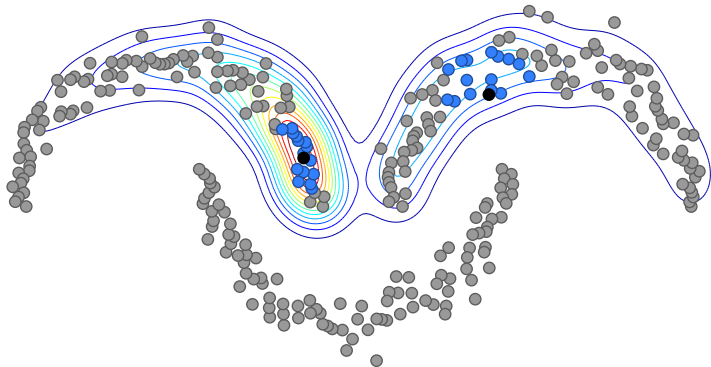
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ranking by conjugate gradient



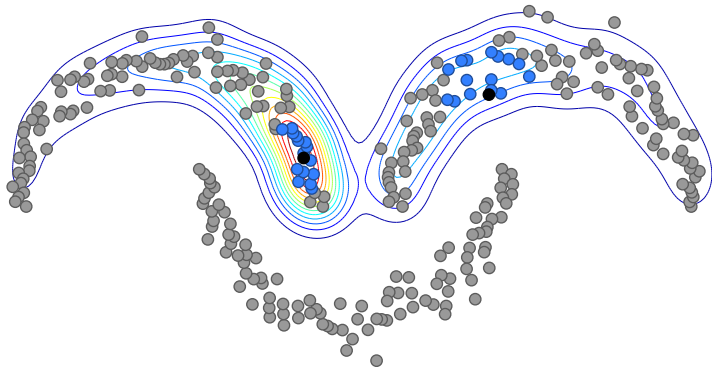
- data points (•), query points (•), nearest neighbors (•)
- iteration 6×2

ranking by conjugate gradient



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- iteration 8×2

ranking by conjugate gradient



- data points (•), query points (•), nearest neighbors (•)
- iteration 9×2

ranking as solving a linear system

- represent image by global descriptor or multiple regional descriptors
- perform initial query based on Euclidean nearest neighbors
- re-rank by solving linear system
- ResNet-101 fine-tuned by BoW + R-MAC + re-ranking:
 - mAP 87.1 (95.8) on Oxford5k, 96.5 (96.9) on Paris6k
 - 1 (21) descriptors/image \times 2048 dimensions

mining on manifolds

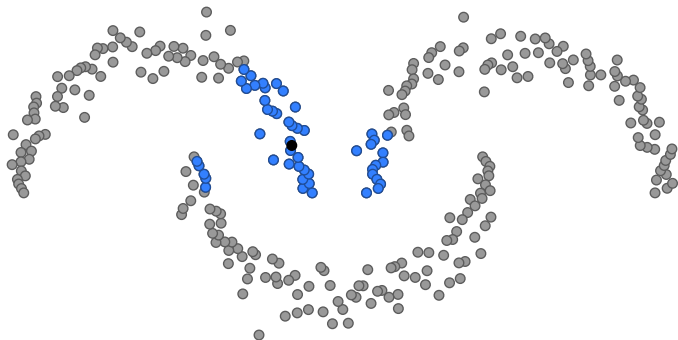
[Iscen et al. 2018]



- data points (\circ), query point x (\bullet)

mining on manifolds

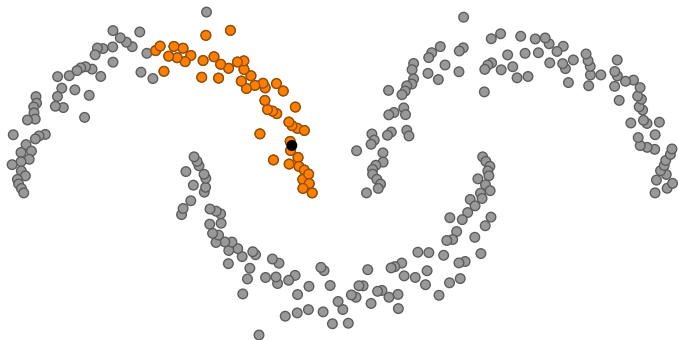
[Iscen et al. 2018]



- data points (\circ), query point x (\bullet)
- Euclidean nearest neighbors $E(x)$ (\circ)

mining on manifolds

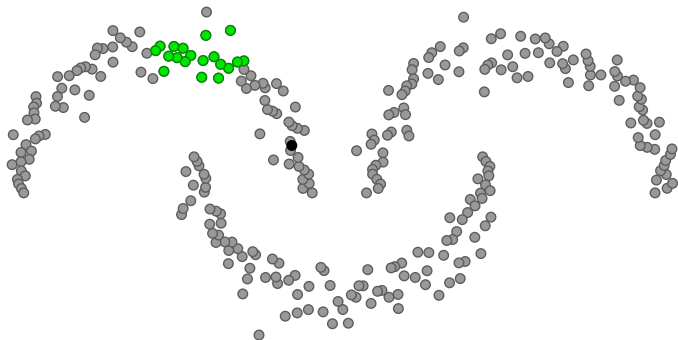
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- data points (\bullet), query point \mathbf{x} (\bullet)
- manifold nearest neighbors $M(\mathbf{x})$ (\bullet)

mining on manifolds

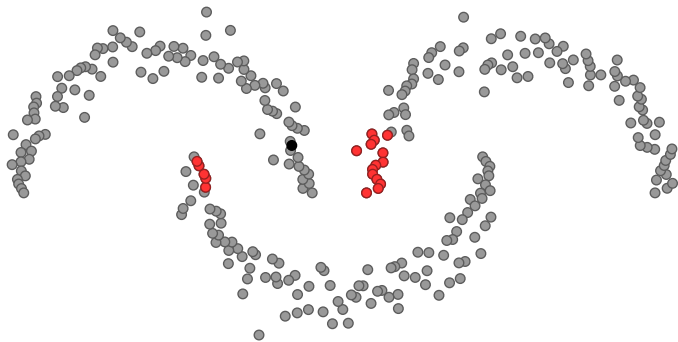
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- data points (\circ), query point \mathbf{x} (\bullet)
- **hard positives** $S^+ = M(\mathbf{x}) \setminus E(\mathbf{x})$ (\bullet)

mining on manifolds

[Iscen et al. 2018]



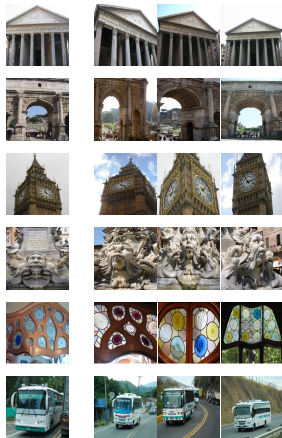
- data points (\circ), query point \mathbf{x} (\bullet)
- **hard negatives** $S^- = E(\mathbf{x}) \setminus M(\mathbf{x})$ (\circ)

mining on manifolds



- query (anchor) (\mathbf{x})
- positives $S^+(\mathbf{x})$ vs. Euclidean neighbors $E(\mathbf{x})$
- negatives $S^-(\mathbf{x})$ vs. Euclidean non-neighbors $X \setminus E(\mathbf{x})$

mining on manifolds



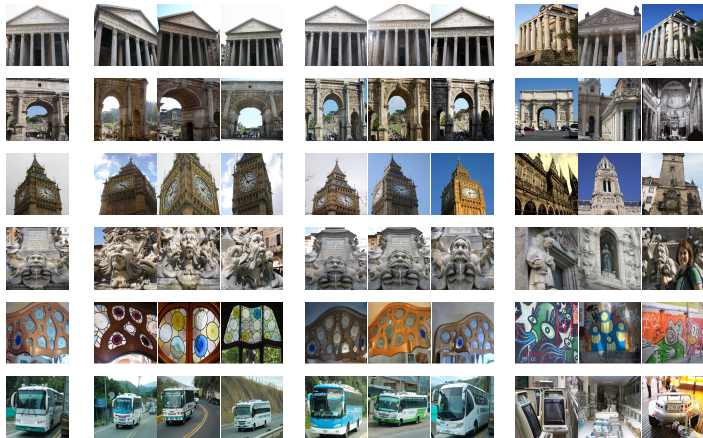
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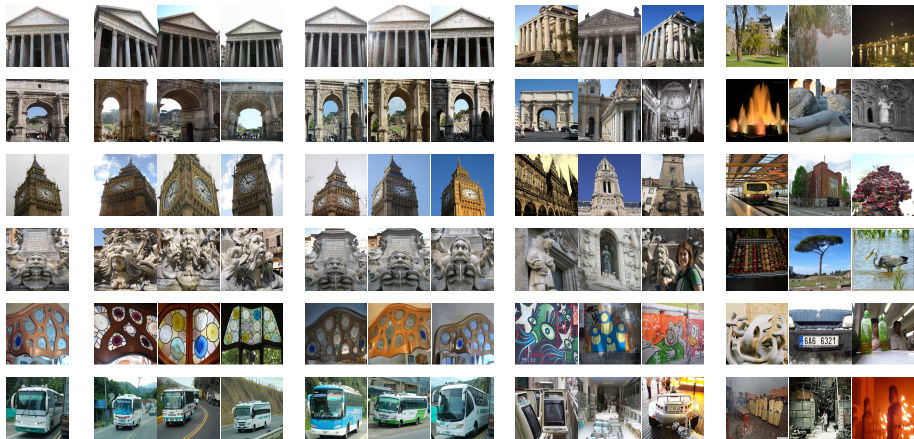
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mining on manifolds

- pre-train network
- extract descriptors on **unlabeled** dataset
- construct nearest neighbor graph
- sample **anchors**, measure Euclidean and manifold distances
- sample **positives** and **negatives**
- fine-tune using **contrastive** or **triplet** loss
- VGG-16 + R-MAC, mAP on Oxford5k (Paris6k):
 - pre-trained on ImageNet: 68.0 (76.6)
 - fine-tuning with SIFT + 3d reconstruction pipeline: 77.8 (84.1)
 - **unsupervised fine-tuning**: 78.2 (85.1)

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summary

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- global descriptors are compact and fast, but do not perform as well as local descriptors
- pooling CNN representations is best at last convolutional layers: MAC, R-MAC, SPoC*, CroW*
- fine-tuning with contrastive or triplet loss allows transferring to a new domain and learning to rank as opposed to classify
- now that images are represented by a global descriptor or just a few regional descriptors, graph methods are more applicable than ever
- modeling the manifold explicitly allows unsupervised fine-tuning without labels, auxiliary systems (e.g. SIFT pipeline), or other information (e.g. temporal neighborhood in video)

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